# Designing Dynamic Reassignment Mechanisms: Evidence from GP Allocation\*

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#### Abstract

Many centralized assignment systems seek to not only provide good matches for participants' current needs, but also to accommodate changes in preferences and circumstances. We study the problem of designing a dynamic reassignment mechanism in the context of Norway's system for allocating patients to general practitioners (GPs). We provide direct evidence of misallocation under the current system—patients sitting on waitlists for each others' GPs, but who cannot trade—and propose an alternative mechanism that adapts the Top-Trading Cycles (TTC) algorithm to a dynamic environment. In contrast to the static case, dynamic TTC may leave some agents worse off relative to a status quo where trades are not permitted, introducing novel concerns about fairness. We empirically evaluate how this mechanism would perform by estimating a structural model of switching behavior and GP choice. While introducing TTC would on average reduce waiting times and increase patient welfare—with especially large benefits for female patients and recent movers—patients endowed with undesirable GPs would be harmed. Adjustments to the priority system can avoid harming this group while preserving most of the gains from TTC.

Keywords: empirical market design, top-trading cycles, dynamic reassignment, waiting

lists, single-payer healthcare JEL Codes: I18, D47, D04

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## I Introduction

Centralized (non-price) assignment mechanisms are used to allocate many important resources in the economy, including schools, jobs, housing, and healthcare. A rich theoretical and empirical literature has studied the design of such mechanisms. Much of this work has focused on providing good matches for participants' current needs. However, in many of these markets, agents' preferences over objects may change over time. Students may wish to transfer schools; public housing residents may want to down-/up-size as household composition changes; workers may want to relocate. Much less is known about how to design markets when there are repeated matching opportunities. Even in markets with sophisticated centralized assignment mechanisms, aftermarkets and reassignment systems are often less carefully designed.

This paper studies the problem of dynamically re-assigning agents to objects, when agents' preferences change over time. We make three conceptual and empirical contributions. First, we provide direct empirical evidence of unrealized gains from trade in an important dynamic assignment market—the market for general practitioners (GPs) in Norway. Second, we propose an alternative mechanism that adapts a standard tool for centralized reassignment—the Top-Trading Cycles (TTC) algorithm—to a dynamic environment, and clarify the incentive and distributional challenges that arise. Finally, we develop and estimate a model of patient preferences and choice over GPs and evaluate counterfactual mechanisms within a dynamic equilibrium model of a patient-GP (re)assignment system.

Our empirical setting is the Norwegian primary care system. As in many national health insurance schemes, every individual in Norway has a formally assigned GP who acts as a first point of contact and gatekeeper to secondary care. In principle, individuals (or hereafter, patients) have free choice of GP. In practice, each GP has a cap on the number of patients they can have on their "panel," creating capacity constraints that limit patients' effective choice of GP. In an effort to facilitate GP switching, in 2016 Norway began allowing patients to join waitlists for oversubscribed GPs while keeping their spot on their current GP's panel. Patients are permitted to stand on at most one GP's waitlist a time, and are then reassigned from the waitlist on a first-come, first-served basis to vacancies on the desired GP's panel.

The starting point for this paper is the observation that strictly enforcing first-come first-served priority and only allowing reassignments when there is a vacancy may substantially limit gains from trade. At any given time, there may be many patients waiting for each others'

<sup>&</sup>lt;sup>1</sup>Similar constraints exist in many primary care systems around the world, as well as in the context of Health Maintenance Organizations (HMOs) in the US.

GPs, but who have no means by which to trade. Indeed, we find that 15 percent of patients on a waitlist in December 2019 (the last month of our data) could be reassigned through a single run of the TTC algorithm, which looks for not only bilateral trades among pairs of patients, but also for "cycles" of trades among an arbitrary number of patients.<sup>2</sup> Moreover, a simple mechanical simulation suggests that if TTC had been run every month since the inception of waitlists—holding patients' GP choices fixed—the number of patients standing on waitlists would have been 23 percent lower at the end of 2019.

Despite clear evidence of unrealized gains from trade, the equilibrium consequences of incorporating TTC into Norway's GP reassignment system are not immediately obvious. In a static setting, TTC is known to be both strategy-proof (meaning it is a dominant strategy for agents to report their preferences truthfully) as well as Pareto-improving (Shapley and Scarf, 1974; Roth, 1982). In a dynamic setting, these results no longer hold. A dynamic mechanism that repeatedly runs TTC is not strategy-proof because patients' choices affect not only which GP they will receive, but also how long they will have to wait.<sup>3</sup> Patients' equilibrium strategic responses to changes in the mechanism may therefore offset the mechanical reductions in waiting time that arise when patients' GP choices are held fixed. Moreover, relative to a status quo with strictly first-come first-served priority, introducing TTC may leave some patients worse off. These patients may experience longer waiting times under TTC because the panel slot they would have taken under the status quo system is instead given to another patient who arrived later, but who can form a trading cycle with the owner of that slot.<sup>4</sup> These dynamic effects reflect a more subtle aspect of TTC: only a patient with an oversubscribed GP (whose endowment is a scarce resource) has the opportunity to trade. Patients with undersubscribed GPs are effectively de-prioritized, and may thus experience systematically longer waiting times. Ultimately, the size of both the average gains from introducing TTC and any associated harms are an empirical question.

The rest of the paper studies the equilibrium impacts of introducing TTC and other related matching algorithms to Norway's existing waitlist system. We address two key empirical

<sup>&</sup>lt;sup>2</sup>For example, suppose patient A is on the waitlist for the GP of patient B, who is on the waitlist for the GP of patient C, who is on the waitlist for the GP of patient A. A three-way exchange ("trading cycle") among the three patients can leave all with their requested GP.

<sup>&</sup>lt;sup>3</sup>Our primary mechanisms of interest maintain the restriction that a patient may stand on at most one waitlist at a time. This amounts to limiting submitted rank-order lists to length two, in which case TTC is not strategy-proof even in a static setting. However, even if patients could submit unrestricted preference lists (as in the canonical TTC mechanism), they would have an incentive to truncate their submitted lists under TTC in the dynamic model we consider. See Section V.E for further discussion.

<sup>&</sup>lt;sup>4</sup>See Appendix B.3 for a stylized example of this phenomenon.

challenges. First, patients' GP choices will likely respond to changes in waitlist lengths as well as to changes in their beliefs about how quickly waitlists will move, both of which may vary across mechanisms. Second, the number of patients standing on waitlists grew rapidly during our sample period (2016–2019). The data are therefore not drawn from a stationary environment, where we ultimately want to make comparisons. Addressing these challenges requires economic modelling on two fronts. We first formulate a demand model of patients' decisions to switch GP. We then introduce a dynamic equilibrium model of a patient-GP reassignment system, which will allow us to predict outcomes in a stationary equilibrium.

We estimate the demand model parameters via a Gibbs' sampler using monthly administrative data on Norway's GP assignment system. Our estimates imply substantial horizontal differentiation across GPs, suggesting large returns to an efficiently designed reassignment system. Much of this differentiation is driven by geographic location, but we also find that patients have strong preferences for a doctor of the same gender (worth the equivalent of 6–7 minutes of travel time) and similar age (1 minute). The estimated attention probabilities closely match switch request rates by age, gender, and whether and how far a patient recently moved. Moves are a particularly important driver of mismatch between patients and their GPs, and strongly predict switch requests. Our preferred specification estimates an annual discount factor of approximately 0.91, consistent with reduced-form evidence that patients' GP choices are responsive to waitlist lengths.

We apply these estimates within a dynamic equilibrium model of Norway's patient-GP reassignment system. Our model is calibrated to match the basic elements of the Norwegian setting, including the distribution of patient and GP characteristics and the rate at which patients age, die, and move between municipalities. We define an equilibrium in which there is a fixed point between patients' beliefs about waiting time and their optimal GP decisions, where beliefs match the long-run stationary distributions generated by optimal behavior. Our simulations imply that under Norway's status quo mechanism, 9 percent of the population would be standing on a waitlist in the stationary equilibrium, and the average patient would expect to wait over a year to switch to their chosen GP.<sup>5</sup>

Our primary counterfactual is to run the TTC algorithm at the end of each month, after all naturally arising vacancies have been filled from waitlists. We find that relative to the status quo, the gains from introducing TTC are equivalent to reducing patients' travel time

<sup>&</sup>lt;sup>5</sup>As of February 2024, 6.5 percent of the population was standing on a GP waitlist, more than twice the number at the end of our sample period. Our prediction that waitlists would continue to grow dramatically is thus qualitatively consistent with what has actually occurred.

to their GP by 0.7 minutes for every patient in the economy. Over half of this improvement (0.4 minutes) is directly due to patients obtaining closer GPs, with the remainder due to better matching on other dimensions. These gains are economically meaningful, representing 14 percent of the upper bound achievable under a benchmark with no capacity constraints. Overall, TTC benefits the majority of patients, and in particular younger and female patients and recent movers, who are most likely to request to switch GPs and to use waitlists.

As in our mechanical simulation, however, some patients are harmed. In particular, patients whose GPs are undersubscribed face longer waiting times and are worse off. This harm is driven both directly by the fact that TTC prioritizes patients with desirable endowments, and indirectly by these patients' resulting increased willingness to wait for the most desirable GPs. Since it may seem unfair to disadvantage patients who already have less desirable GPs, we consider two alternative mechanisms intended to mitigate these distributional consequences. First, we implement the patient-proposing deferred acceptance (DA) algorithm instead of TTC. This mechanism strictly respects first-come first-served waiting time priority, and thus does represent a Pareto improvement relative to the status quo.<sup>6</sup> However, it produces almost negligible gains, illustrating a fundamental trade-off between respecting first-come first-served priority and exploiting gains from trade. Second, we implement a "TTC with priority" (TTCP) algorithm that prioritizes patients with undersubscribed GPs for panel vacancies.<sup>7</sup> The results are encouraging. TTCP achieves 61 percent of the welfare gains from TTC, while leaving patients with undersubscribed GPs just as well off as under the status quo.

In a final analysis, we compare Norway's current mechanism to one in which there are not formal waitlists to ration excess demand for GPs. Specifically, we simulate a mechanism in which patients may only choose from among GPs that have open slots at the moment they consider switching, meaning there is a substantial degree of "luck" involved.<sup>8</sup> Strikingly, mean patient welfare is slightly *higher* than under Norway's current mechanism. However, median welfare is lower. The gains from eliminating waitlists are concentrated among a minority of patients who are highly mismatched with their current GP. These patients prefer

<sup>&</sup>lt;sup>6</sup>DA is distinct from Norway's status quo mechanism because DA allows trades among patients at the top of each waitlist, whereas Norway's system requires a vacancy before any reassignments can be made.

<sup>&</sup>lt;sup>7</sup>This proposal is similar in spirit to the priority given to blood type O patients for blood type O donors in organ allocation. We are grateful to Al Roth and Itai Ashlagi for this suggestion.

<sup>&</sup>lt;sup>8</sup>Importantly, this simulation does not allow patients to "check back later" if their desired GP is not available when they first consider switching, which would add an element of patient effort to the rationing mechanism. We therefore view this simulation as simply a suggestive benchmark for what a "no waitlists" environment might look like. See Section V.E for further discussion.

an environment with more limited choice and no waiting times, whereas most patients prefer the ability to choose from a wider set of GPs. While suggestive only, these findings may partly explain why waitlists are rarely seen in other primary care systems. Our proposals of TTC and TTCP can be viewed as practical proposals to reduce waiting times while also keeping the benefits from the increased choice that waitlists afford.

Related Literature. This paper contributes to a growing empirical literature on the design of centralized allocation mechanisms. In studying dynamic reassignment, we build on two specific strands of prior work. The first is static reassignment, in which all agents and objects are matched at a single point in time, and agents may have an endowed object. Canonical examples are the housing allocation problem with existing tenants and paired kidney exchange (Shapley and Scarf, 1974; Abdulkadiroğlu and Sönmez, 1999; Roth, Sönmez and Ünver, 2004). In this context, the TTC algorithm is known to be efficient and strategy-proof (Ibid.). These properties motivate our proposal to adapt TTC to a dynamic environment, but as we will demonstrate, may break down when participants face dynamic incentives. The second is dynamic assignment, in which agents and objects arrive stochastically over time, but agents do not arrive with endowments. Examples include waitlists for public housing (Waldinger, 2021; Lee, Ferdowsian and Yap, 2024), deceased donor kidneys (Agarwal et al., 2021), and hunting licenses (Verdier and Reeling, 2022). Like in our setting, the trade-off for participants between shorter waiting times and a preferred assignment is central to the optimal design of such mechanisms, as well as in revealed preference analysis of choice data.

In the context of dynamic reassignment, Combe et al. (2022) study the reassignment system for French teachers in an infinite horizon environment, but model teachers as truthfully reporting their (static) preferences. Narita (2018) and Kapor, Karnani and Neilson (2024) study models of school choice with aftermarkets in which agents can exhibit forward-looking behavior, but limit consideration to two periods. Our work builds on these studies by considering

<sup>&</sup>lt;sup>9</sup>TTC has also been applied in settings of *static assignment* in which agents do not have endowments, particularly in the context of school choice (Abdulkadiroğlu and Sönmez, 2003; Pathak and Sethuraman, 2011; Leshno and Lo, 2020). This literature highlights a tension between efficiently assigning students and respecting school priorities, which features prominently in our setting.

<sup>&</sup>lt;sup>10</sup>Several theoretical papers study how dynamic incentives impact the optimal design of dynamic assignment mechanisms (e.g., Su and Zenios, 2004; Bloch and Cantala, 2017; Arnosti and Shi, 2020; Baccara, Lee and Yariv, 2020; Leshno, 2022; Che and Tercieux, 2023). To our knowledge, there is no theoretical characterization of optimal mechanisms for the class of dynamic reassignment models we consider. Existing theoretical work largely abstracts from strategic behavior, or focuses on a limited form of agent heterogeneity (Ashlagi, Nikzad and Strack, 2022; Akbarpour, Li and Gharan, 2020; Akbarpour et al., 2023; Combe, Tercieux and Terrier, 2022). Work that has considered strategic behavior largely focuses on characterizing strategy-proof and stable mechanisms (Narita, 2018; Feigenbaum et al., 2020; Pereyra, 2013).

the combination of an infinite horizon and forward-looking agent behavior, which raises a new set of issues regarding how agents think about waiting times. Larroucau and Ríos (2022) also study a setting (college major choice) in which both these elements are present. Their focus is on learning and congestion externalities (without the possibility of waitlists), while our focus is on finding gains from trade and the distributional issues that arise (when agents may choose to wait). Waiting time is a natural market-clearing mechanism for processing reassignments in a number of other related settings (e.g., public housing, public schools, university parking spots), and our study represents a first step in understanding its equilibrium implications.

Finally, as in other countries, the existence of a national health insurance scheme in Norway motivates using a non-price mechanism to allocate healthcare resources at the point of service. Our paper contributes to a literature studying the optimal design of such mechanisms, and is among the first to bring the tools of market design to bear on this topic. The existing literature has largely focused on service-level allocation, in which context early work studied whether limiting capacity and running waitlists for non-emergency services could deter low-value care (Nichols, Smolensky and Tideman, 1971; Propper, 1990, 1995; Gravelle and Siciliani, 2008b). Subsequent work has studied the design of prioritization schemes on such waitlists (Gravelle and Siciliani, 2008a; Shen et al., 2020; Gruber, Hoe and Stoye, 2023) as well as the relative merits of price versus waiting times as the rationing mechanism (Russo, 2023). Our work, in contrast, considers the issue of provider-level allocation, where the potential for repeated interactions raises the issue of whether patients may wish to be reassigned. In a setting closely related to ours, Mark (2021) studies the Canadian primary care system, in which the process for switching GPs is decentralized and patients who wish to do so must exert costly effort to find vacancies. We see our work as complementary in that we study the design of a centralized mechanism, allowing us to apply tools from the field of market design.

The paper proceeds as follows. Section II introduces our setting and data and demonstrates the existence of gains from trade among waiting patients. Section III presents the structural model of patient attention and GP choice. Section IV describes our estimation procedure and parameter estimates. Section V presents our counterfactual simulations, and Section VI concludes.

## II Background, Data, and Descriptive Evidence

### II.A Empirical Setting

Norway has a comprehensive national health insurance scheme primarily financed by general taxation. Patient cost-sharing at the point of service is nonzero for most outpatient care, but is still limited. Healthcare utilization is primarily managed via supply-side forces. Central among these forces is a gate-keeping system whereby patients need a referral from a primary care provider before receiving specialist care. Such providers therefore play a central role in the healthcare system.

Primary care is almost exclusively provided by GPs.<sup>11</sup> GP care is organized via a patient panel system, whereby every person enrolled in the national health insurance scheme is assigned to a specific GP. Patients enrolled on a given panel are in general only permitted to visit that GP for their primary care needs.<sup>12</sup> Similar primary care systems exist in Canada, Great Britain, Italy, and Sweden (among other countries), as well as in the context of Health Maintenance Organizations (HMOs) in the US. The key reason for maintaining a centralized administrative linkage between a patient and a specific GP is to allow for a "capitated" payment model, under which GPs receive a fixed payment for each person enrolled on their patient panel. Norway uses a partially capitated payment model, meaning GPs receive a fraction of their revenue from capitated payments (on average 30 percent) and the remainder from fee-for-service payments.

The supply of GPs is regulated through a fixed number of government contracts.<sup>13</sup> Similar to Medicare and Medicaid physician contracts in the US, government contracts involve take-it-or-leave-it payment terms, with some exceptions made to attract physicians to rural areas. One important difference in Norway is that at the time a GP enters into a government contract,

<sup>&</sup>lt;sup>11</sup>As of 2023, nurses in Norway do not have prescribing or referring authority outside of a few special cases. While it is common for nurses to handle well visits for children and adolescents, adult patients must typically consult a GP for the majority of their primary care needs (Robstad et al., 2022; Hansen, Boman and Fagerström, 2020). Primary care needs could include periodic well-visits, non-urgent sick visits, obtaining prescriptions or referrals to specialist care, or receiving documentation for sick leave through the national sick leave scheme.

<sup>&</sup>lt;sup>12</sup>There are some exceptions; for example, patients have the right to seek a second opinion from another GP on a matter already discussed with their own GP.

<sup>&</sup>lt;sup>13</sup>While GPs can also practice outside of the national health insurance scheme, the market for private practice primary care remains small or non-existent in most of the country (The European Observatory On Health Systems and Policies, 2023)

both parties must agree on a maximum number of patients that the GP's panel can take.<sup>14</sup> In entering into the contract, the GP agrees to take on a workload sufficient to serve all patients that enroll on their panel, up to the agreed panel cap. GPs are required to be able to provide an appointment to patients within 5 working days, which in part motivates the existence of panel caps (Lovdata, 2012).

Patients make GP enrollment elections via a nationally centralized online platform.<sup>15</sup> The system operates on a rolling basis, without any special enrollment periods or forced reenrollment decisions. Enrollment changes take effect on the first day of the next month, and GPs have no way to control which patients enroll on their panel. When a GP retires or quits, patients receive six months' notice and can either switch GP or remain on the panel of the replacement GP.<sup>16</sup> Newborns are by default assigned to their mother's GP, regardless of whether the panel cap is violated. Every patient is thus assigned to a GP panel at all times.

While patients in principle have free choice over GPs, in practice the panel caps generate capacity constraints. A GP with no open slots on their panel is listed as "unavailable" on the online enrollment platform. Patients that wish to switch GP immediately may therefore only choose among the set of GPs with open slots on their panels (henceforth, "open panels"). Prior to 2016, a patient would simply need to check back later if their desired GP was unavailable. <sup>17</sup> In November 2016, a new functionality was introduced whereby patients could join a waitlist. Patients are permitted to join only one waitlist at a time, but can switch which waitlist they are on as often as they would like. <sup>18</sup> Panel slots that become available are filled from the waitlist on a first-come, first-served basis, according to when each patient joined that waitlist. Once a patient joins a waitlist, they commit to being reassigned to the target GP once they reach the front of the list; there is no opportunity to renege except to remove oneself from the waitlist before it is too late.

<sup>&</sup>lt;sup>14</sup>Operationally, local municipal governments work with GPs to set panel caps and negotiate any other idiosyncratic features of a GP's contract, such as reduced working hours or coverage for parental leave spells.

<sup>&</sup>lt;sup>15</sup>The online platform is publicly available at https://tjenester.helsenorge.no/bytte-fastlege. Appendix Figure A.1 provides a screenshot of the interface. Patients are permitted to switch GPs at will up to two times per year (though this constraint rarely binds), with additional switches granted for qualifying life events.

<sup>&</sup>lt;sup>16</sup>If the replacement GP has a lower panel cap, a randomly selected subset of patients are administratively reassigned, without their explicit consent, to another GP in the local area.

<sup>&</sup>lt;sup>17</sup>In fact, a cottage industry arose of private companies that automated the process of monitoring the central web platform for when GP panel slots became available and selling an email/text alert service to consumers for a monthly fee.

<sup>&</sup>lt;sup>18</sup>The centralized web platform provides real-time information on the number of patients on each waitlist, and if a patient is logged in, on their current position on the waitlist they are standing on (see Appendix Figure A.1).

#### II.B Data

Our data are derived from two main sources. First, we observe detailed administrative data on the GP assignment system itself (*Fastlegedatabasen*). These data include a full history of patient enrollment, waitlist spells, and GP characteristics. We can therefore reconstruct the state of each GP's panel and waitlist at any point in time. Second, we link these data to register data from Statistics Norway on individual demographics, including age, gender, family relationships, income, education, and monthly municipality of residence. Further details are provided in Appendix A.1. We have data for the period 2014–2019.

Figure 1 shows the number of GP switches and waitlist use over time. GP switches take one of two forms: (i) standard switches to an open panel, and (ii) switches that occur once an individual reaches the front of a waitlist and is reassigned. Between 2014 and 2019, there were an average of 5,259,076 patients per month in the GP allocation system. An average of 31,856 patients (0.6 percent) switched their GP each month. Once waitlists were introduced in November 2016, an average of 28 percent of switches were executed via a waitlist, whereas the remaining 72 percent were switches to an open GP panel. The total number of switches per month did not change dramatically. The waitlists have grown steadily since their introduction. By the end of 2019, 133,538 people were standing on a waitlist (2.5 percent of all patients). As of February 2024, this number had risen to 326,506 (6.5 percent of all patients).

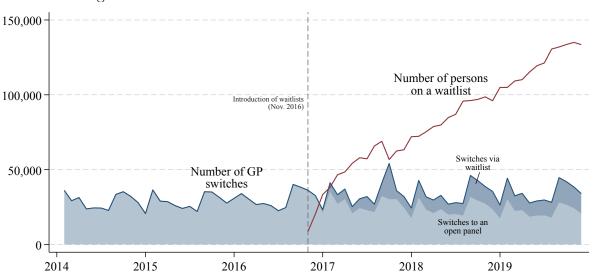


Figure 1. Number of GP Switches and Waitlist Use Over Time

Notes: The figure shows the number of GP switches per month and the stock of individuals standing on a waitlist each month between 2014 and 2019, including both adults and children. GP switches are decomposed into standard switches to an open GP panel (light blue) and switches that occur only after going through a waitlist (dark blue).

Patients. Our primary restriction on patients is to exclude those who are under 16 years old. Children's interactions with the healthcare system, including GP enrollment, are formally managed by parents until a child turns 16. There are also special exceptions given to children that allow them to bypass GP panel caps in certain situations, as well as to switch GPs alongside a parent without themselves going through a waitlist. As these factors would substantially complicate our analysis, we limit our focus to the experience of adults.

Table 1 provides summary statistics on patients, focusing on the three-year period from 2017 to 2019. The sample is an unbalanced panel at the patient-month level (panel entry occurs at age 16 or immigration; panel exit occurs at death or emigration). The first column describes the full sample. There are 4.78 million unique patients, representing the universe of over-16 individuals registered as resident in Norway and covered under the national insurance scheme. Patients are on average 47 years old and earn 425,374 NOK annually. Just over 7 percent of individuals are temporary residents, 32 percent have post-secondary education, and 10 percent moved to a new municipality at least once during 2017–2019.

In terms of GP choice, 19 percent of patients requested to switch their GP at least once (4 percent of patients did so more than once). The average travel time (by car) to a patient's GP was 10.7 minutes; the median was 5.8 minutes.<sup>19</sup> More than half (58 percent) of patients have a GP of the same gender as themselves. In terms of waitlist use, 9 percent of individuals were at any point on a waitlist over this period. Conditional on ever being on a waitlist, the average number of months on a waitlist was 6.5.

The remaining three columns of Table 1 break up the full patient sample into three subgroups: (i) patients who never switched their GP nor joined a waitlist, (ii) patients who switched GP but never joined a waitlist, and (iii) patients who joined a waitlist (and may or may not have successfully switched their GP). Several patterns are apparent. First, gender homophily appears to be a driver of switching behavior. While 56 percent of patients on waitlists currently held a GP with the same gender as themselves, 64 percent of them were waiting for a GP of the same gender. Waiters are also disproportionately female, which could be driven by a scarcity of female GPs or a stronger gender homophily preference among female patients.

Second, there is a striking pattern with respect to moves. Among patients who never requested to switch their GP, only 6 percent of individuals moved municipality during this

<sup>&</sup>lt;sup>19</sup>Travel time is measured between the population-weighted centroid of patients' municipality of residence and the address of their GP's office.

Table 1. Patient Summary Statistics

	Full	Never use	Ever	
Sample demographic	Sample	Never switched	Ever switched	
Number of individuals	4,780,647	3,875,753	497,111	407,783
Pct. of individuals		0.81	0.10	0.09
Demographics				
Pct. female	0.50	0.48	0.51	0.64
Age	47	49	40	42
Pct. with post-secondary education	0.32	0.31	0.32	0.37
Annual income (000 NOK)	425	437	358	390
Pct. temporary resident	0.07	0.07	0.08	0.08
Pct. rural	0.30	0.31	0.30	0.28
Pct. ever moved	0.10	0.06	0.34	0.26
Choice of GP				
Pct. ever switched to open GP	0.13	_	1.00	0.28
Travel time to current GP (min.)	10.7	9.5	17.1	14.3
Pct. with GP of same gender	0.58	0.57	0.59	0.56
Use of waitlists				
Pct. ever on a waitlist	0.09	_	_	1.00
Number of months on a waitlist $  > 0$	6.5			6.5
Pct. waiting for GP of same gender	0.64			0.64
Travel time to wl. GP – curr. GP (min.)	-6.8			-6.8

Notes: The table provides summary statistics on adult patients present in the data from 2017–2019. Except where otherwise specified, all values in the table represent means over patient-months. "Ever" means at any point during 2017–2019. Moves are counted only if they are across municipalities. Age, gender, education, and income data are not available for temporary residents, so those means are only among permanent residents.

period. Among those who switched GP but never used a waitlist (meaning they switched to an open GP), 34 percent of individuals moved. Among those who used a waitlist, 26 percent moved. These facts suggest that geographic proximity is an important factor in GP choice. The even higher move rate among patients who only open-switched is consistent with patients who are far from their current GP being less selective, i.e., more likely to simply settle for an open GP. Finally, the last row of the table shows that among patients who used a waitlist, the waitlist GP was on average 6.8 minutes closer than their current GP (on a base of 14.3 minutes travel time to current GP).

**GPs.** Table 2 provides summary statistics on the 6,470 GP panels active during 2017-2019. As with patients, the data consist of an unbalanced panel at the GP panel-month level.<sup>20</sup> There is an important distinction between a *GP panel* and a *GP*. A GP panel is the administrative unit to which patients are actually linked. Each panel is then served by a GP (a licensed

 $<sup>^{20}</sup>$ The average GP panel appears in the data for 28 months (out of 36 possible). At a given time, between 4,840 and 5,106 panels are in operation.

medical doctor). The GP that serves a given panel may change over time, independently of the patients enrolled on that panel.

The first column of Table 2 describes the full set of GP panels. The average panel had a cap of 1,138 patients and had available slots for 36 percent of months. Across all months between 2017 and 2019, the average GP serving these panels was 47 years old, 42 percent of GPs were female, and 11 percent were temporary GPs.<sup>21</sup> The average GP panel-month had 18 people standing on its waitlist, and the average enrollment-to-cap ratio was 94 percent.

Table 2. GP Panel Summary Statistics

	All	Undersubscribed	Oversubscribed
Number of GP panels	6,470	3,532	2,938
Pct. of GP panels	1.00	0.55	0.45
Panel characteristics			
Enrollment cap	1,138	1,143	1,135
Pct. months with available slots	0.36	0.70	0.06
Pct. rural	0.37	0.44	0.30
GP demographics			
Age	47	47	48
Pct. months with female GP	0.42	0.34	0.50
Pct. months with temporary GP	0.11	0.15	0.08
Panel enrollment stats.			
Num. enrollees on a waitlist	18	21	14
Num. waiting on waitlist	18	4	30
Num. enrollees / cap	0.94	0.87	1.00

Notes: The table provides summary statistics on the set of GP panels present in the data from 2017–2019. Except where otherwise specified, all values in the table represent means over GP panel-months. Oversubscribed GP panels are those which are at capacity for more than 75 percent of months. Enrollment and waitlist use statistics reflect the full population (including children under 16).

The remaining two columns of Table 2 separate GP panels into two subgroups: (i) those that were not consistently oversubscribed, and (ii) those that were. We define "consistently oversubscribed" to mean that a given GP panel was at capacity for more than 75 percent of the months that it appeared in the data from 2017–2019. There are several notable patterns. First, GP panels in urban areas and those served by female GPs are more likely to be oversubscribed, while GP panels served by temporary GPs are more likely to be undersubscribed. Second, among the current enrollees of undersubscribed panels, an average of 21 patients (2.1 percent of enrollees) were themselves standing on a waitlist (and therefore trying to leave the panel).

<sup>&</sup>lt;sup>21</sup>Temporary GPs (*vikar*) are used while the primary GP (*fastlege*) is on parental leave or while the position is vacant and the municipality is actively searching for a new permanent GP.

Among oversubscribed panels, this is true for fewer patients—an average of 14 people per panel (1.2 percent of enrollees). Thus, while some GPs are systematically more demanded than others, there are still many patients requesting to switch away from over-demanded GPs. Finally, capacity utilization in the system is high. Even for consistently undersubscribed GPs, 87 percent of panel slots were occupied.

#### II.C Prevalence of Double Coincidence of Wants

We now provide direct evidence of unrealized gains from trade among patients on Norway's GP waitlists. This prima facie evidence motivates the structural model and counterfactual simulations developed in the remainder of the paper.

Static Gains From Trade. Norway's current GP allocation system does not permit trades among patients standing on waitlists. Even when two people are each at the front of the waitlist for the other's GP, this "trade" cannot occur until there is a vacancy on one of the two panels, allowing one waiting patient to vacate their spot for the other. Note that the same problem exists in a mechanism without formal waitlists. Two individuals could simultaneously check to see if there was an opening at one another's GP, see that there was not, and not be able to trade. The advantage (from the analyst's perspective) of the waitlist system is that we have a record of these preferences. In particular, we are able to observe whether there are individuals who would want to trade with one another.

Using the waitlists data, we begin by calculating the extent to which such "double coincidence of wants" exist. We search for possible trades using the Top Trading Cycles algorithm (Shapley and Scarf, 1974; Abdulkadiroğlu and Sönmez, 1999). We first run the algorithm on the waitlists from the last month of our data, December 2019. At the end of this month, there were 133,332 individuals standing on a waitlist. These waiters were currently enrolled on almost every existing GP panel (4,963 out of 5,010), but were standing on the waitlist for only 3,695 unique GPs.<sup>22</sup>

The TTC algorithm takes two primary sets of inputs: (i) the set of participating agents and their rank-order preference lists over objects, and (ii) the set of participating objects and their rank-order priority lists over agents. In our setting, agents (patients) have preference lists of length at most two. Patients standing on a waitlist first prefer their waitlist GP, and then their current GP. Patients not standing on a waitlist prefer only their current GP. Objects (GPs)

 $<sup>^{22}\</sup>mathrm{Appendix}$  Figure A.2 provides a histogram of waitlist lengths across these 3,695 waitlists.

first prioritize all patients currently on their panel (guaranteeing each patient an assignment no worse than their current GP), and then prioritize the patients on their waitlist in descending order of waiting time.<sup>23</sup> We run the algorithm and find that 20,377 people (15 percent of waiters) could have been immediately reassigned via TTC.<sup>24</sup> Appendix Table A.1 describes the types of adult patients that could be immediately reassigned. Reassigned patients tended to have a larger difference in travel time between their current and waitlist GPs, consistent with location preference heterogeneity being a key driver of gains from trade.

The fact that gains from trade exist tells us that patients must differ—at least to some extent—in their preferred GP. We explore the sources of this horizontal preference heterogeneity descriptively using a conditional logistic regression predicting which GP a patient chooses, conditional on making a switch request. Appendix B.2 provides a detailed description of these results. We find that indeed, the most important source of horizontal preference heterogeneity is patients geographic location relative to GP offices. We also find patients have a preference for a same-gender and similar-age GP.

Impact on Evolution of Waitlists. The static analysis suggests that the gains from trade among patients with oversubscribed GPs may be substantial. The welfare impact of these trades, however, will depend on the extent to which they affect patients' waiting times and GP assignments in a dynamic environment. We can begin to get a sense of these dynamic effects through a simple mechanical simulation of how the waitlist would have evolved if trades were processed periodically in the first three years the waitlists were operational. From November 2016 through December 2019, we run the TTC algorithm on the remaining waitlists at the end of each month. Importantly, patients' actions—GP switch requests—are held fixed. We then compare the number of reassignments and waiting times to those under the status quo mechanism.<sup>25</sup>

Figure 2 presents the results of this exercise, comparing the status quo waitlists mechanism (Waitlists) to the counterfactual monthly implementation of Top-Trading Cycles (TTC). Panel (a) shows the number of people on waitlists each month. By the end of 2019, there would have been 23 percent fewer waiting patients under TTC. Panel (b) shows the realized waiting

 $<sup>^{23}</sup>$ Appendix B.1 describes the algorithm we use to find and clear cycles, as well as other implementation details.

<sup>&</sup>lt;sup>24</sup>There is substantial geographic heterogeneity in the fraction of waiters that could be reassigned. In rural Åsnes municipality, it is only 2 percent (out of 420 waiters, where waiters represent 6 percent of the population). In urban college town Bergen, it is 26 percent (out of 7,991 waiters, where waiters represent 3 percent of the population).

<sup>&</sup>lt;sup>25</sup>We compare simulated outcomes under the status quo mechanism to simulated outcomes under the TTC mechanism. Appendix B.1 provides additional details about the implementation of this analysis.

times. The blue series shows the average elapsed waiting time among the stock of individuals standing on waitlists each month, while the red series shows the average waiting time among the flow of individuals successfully reassigned from a waitlist each month. Among reassigned patients, average waiting times would have been 29 percent shorter under TTC, suggesting that trades generated by TTC may lead to significant reductions in waiting times.

(a) Number of Persons on Waitlists (b) Realized Waiting Times 120 Waitlists Among stock of waiters 100 Number of persons (000s) 80 Months Waitlists 60 40 Among those successfully reassigned 20 2017 2018 2018 2019 2019 2020 2017 2020

Figure 2. Results of Running TTC on Historical Data

Notes: The figure shows outcomes from a mechanical simulation in which TTC is run each month on the historical waitlists data, holding all patient actions fixed. Panel (a) shows the number of persons standing on waitlists each month. Panel (b) shows the average elapsed waiting time among the stock of patients standing on waitlists each month (blue) and the average waiting time among the flow of patients who were successfully reassigned from a waitlist each month (red).

While TTC reduces average waiting time, it does not offer a Pareto improvement relative to the status quo. Some patients are harmed in the form of longer waiting times. This can happen because a slot that would have been taken by the first person on the waitlist might be filled earlier by a different patient who is further back on the waitlist but participated in a cycle with the patient previously in that slot. Appendix B.3 provides stylized examples of this phenomenon in our setting. Appendix Figure A.3 shows the distribution of waiting time differences among patients in our simulation. A minority of patients (4.5 percent) have longer waiting times under TTC because they are effectively de-prioritized relative to the status quo.

While this analysis suggests there could be significant welfare gains from introducing TTC, it has two important limitations. First, the simulation holds patient behavior fixed. If the implementation of TTC changed the distribution of waitlist lengths, patients might have requested different GPs. Indeed, the reduced form analysis in Appendix B.2 shows that patients'

choice of GP is responsive to waitlist length. Moreover, if patients understand that TTC may allow them to be reassigned faster, expected waiting times would fall even conditional on waitlist lengths, again potentially influencing patient choices. A second limitation of this analysis is that the market was far from a steady state during our sample period. Use of waitlists rose rapidly after their introduction, and has continued to do so after the end of our sample. The long-run stationary distribution of Norway's GP allocation system—and the associated impact of introducing TTC—may be different when queues are systematically longer. Our counterfactual simulations will rely on a stationary demographic evolution and GP switching process, allowing us to evaluate the impacts of TTC in a long-run equilibrium.

## III Model of GP Preferences and Choice

Section III.A presents a model of attention and GP choice that will form the basis of our strategy to estimate patient demand for GPs. Section III.B then presents a belief model under which patients map waitlist lengths into beliefs about waiting time, which will be an important input into patients' GP choices.

### III.A Attention, Preferences, and Choice

Patients are indexed by i, GPs by j, and time by t. Time is continuous. We model patient preferences at the time they consider switching GPs. At time t, patient i's preferences are represented by indirect flow utilities from being assigned to each GP  $\mathbf{v}_{it} \equiv (v_{i1t}, ..., v_{iJt}) \in \mathbb{R}^J$  and a discount rate  $\rho$ . The patient has observable attributes  $X_{it}$  and is currently assigned to GP  $j_{0t}$ . Going forward, we suppress t subscripts when they do not affect the exposition.

A patient "pays attention" and considers switching GPs at Poisson rate  $p_{it}^{\lambda}$ . When a patient is attentive, two things happen: (i) she draws new preferences  $\mathbf{v}_{it} \sim F(\cdot \mid X_{it})$ , and (ii) she decides whether to switch GP and, if so, to which one. A patient might pay attention due to an event we observe, such as a recent move, or for reasons we do not observe, such as a health event or an interaction with their GP. We model the attention rate  $p_{it}^{\lambda}$  as a function of observables  $X_{it}$  and assume attention follows a memoryless Poisson process, so paying

<sup>&</sup>lt;sup>26</sup>In practice, because our data are at the monthly level, we will estimate monthly attention probabilities and assume that patients can only be attentive once within a month. In reality, patients do make GP selections continuously throughout the month, and our counterfactuals will simulate within-month patient arrival times.

attention at time s does not predict attention at t > s conditional on  $X_{it}$ .

Attentive patients consider the waiting time for each GP, but do not anticipate future preference changes or switching opportunities. If patient i must wait  $T \geq 0$  periods to be assigned to GP j, the net present value of requesting this GP is

$$\int_{\tau=0}^{T} e^{-\rho\tau} v_{ij_0} d\tau + \int_{\tau=T}^{\infty} e^{-\rho\tau} v_{ij} d\tau = \frac{1}{\rho} \left[ v_{ij_0} + e^{-\rho T} (v_{ij} - v_{ij_0}) \right]. \tag{1}$$

Equation 1 shows that the value of switching to another GP can be decomposed into two parts. The first is the value of being forever assigned to their current GP  $j_0$ . The second is the *incremental* value of being assigned to GP j instead of  $j_0$  at some point in the future, discounted by waiting time T. Only the second term depends on the chosen GP j.

It remains to specify patients' information and beliefs about waiting time. The online GP choice interface displays whether each GP has open slots at time t and, if not, the number of individuals on the waitlist for each GP. Let  $\mathbf{w}_{it} = \{w_{i1t}, ..., w_{iJt}\} \in \mathbb{N}_+^J$  denote patient i's position if she joined each waitlist. If a GP has open slots or patient i is already on their panel, i's waitlist position is zero. Letting  $\mathcal{J}_{it}$  denote patient i's choice set at time t, her choice problem can then be written

$$\max_{j \in \mathcal{J}_{it}} \mathbb{E}\left[e^{-\rho T_{ij}} \mid \mathbf{w}_{it}\right] \left(v_{ijt} - v_{ij_0t}\right). \tag{2}$$

This choice problem maximizes the value of being assigned to GP j after some waiting time  $T_{ij}$ , accounting for uncertainty in waiting time given current waitlist lengths and acknowledging that the patient will remain with her current GP while waiting.

This formulation has several implications. First, there is no explicit cost of waiting. The distaste for waiting time arises only due to exponential discounting. An attentive patient will therefore always request to switch to another GP as long as there is *some* other GP in the choice set that delivers higher flow utility than the patient's current GP, regardless of wait time. Our model thus interprets any switch request in the data as implying both that (i) the consumer received an attention shock, and (ii) the requested GP is preferred to the current GP. Any patient who does not request to switch, on the other hand, may be either simply inattentive, or else attentive but prefer their current GP to all others. A second implication of our model is that patients do not necessarily request to switch to their most-preferred GP, in the sense of delivering the highest flow utility. A patient may choose a less preferred GP with a shorter waitlist in order to wait for less time. Finally, an attentive patient who is relatively

satisfied with her current GP is less likely to request to switch. But conditional on requesting to switch, such a patient is more likely to be willing to wait for her most-preferred GP, due to a high "outside option" while waiting.

**Discussion of Modeling Choices.** The goal of our model of attention and GP choice is to predict how patients might change their behavior when faced with different waitlist lengths and beliefs about waiting time under alternative waitlist mechanisms. A number of our modeling choices warrant specific discussion.

First, we choose to focus on inattention rather than switching costs as the explanation for why GP switch requests are infrequent within patient. This choice is not without loss of generality. A model with switching costs would predict that more patients would request to switch should aggregate waiting times fall, while a model of exogenous inattention would not.<sup>27</sup> We choose to neutralize this channel and focus only on exogenous inattention because GP switch request rates do not appear to respond to local changes in aggregate waiting times. Specifically, we test in the data whether the number of switch requests responds to short-run changes in the average waitlist lengths of all nearby GPs, exploiting a technical change in the reassignment algorithm made during our sample period. Appendix B.5 presents this analysis. We do not find any evidence that patients are more likely to request to switch when waitlists for nearby GPs are particularly short. While we cannot rule out the possibility of a longer-term increase in switch requests as patients become aware that the mechanism has improved, the evidence points toward focusing on modeling which GP a patient requests, rather than the decision to switch at all.<sup>28</sup>

Second, our formulation of the choice problem rules out behaviors that would be optimal if patients were fully forward-looking. In particular, patients do not anticipate future preference changes and switching opportunities; they choose a GP as if it will be permanent. This assumption is relatively innocuous for estimation because switch requests are rare at the individual level, and because the identity of a patient's current GP does not affect their ability to switch GPs under the current system. The assumption is stronger, however, for a counterfactual mechanism with TTC. Because patients' expected waiting times will depend on whether their current GP is oversubscribed, they may consider not only a GP's current value,

<sup>&</sup>lt;sup>27</sup>Several papers have considered both exogenous inattention and endogenous switching behavior as explanations for persistent choices (Ho, Hogan and Scott Morton, 2017; Hortacsu, Madanizadeh and Puller, 2017; Abaluck and Adams-Prassl, 2021; Heiss et al., 2021).

<sup>&</sup>lt;sup>28</sup>Note that in our counterfactual simulations, the number of switch requests is still endogenous because the mechanism may change patients' current GPs when they consider switching. If a patient's current GP is preferable to all others when they are attentive, they will not request to switch.

but also its future "trading value." In our view, it is unlikely that patients would systematically engage in this type of behavior. Since switch requests are rare, a GP's trading value is limited by the fact that any gain from modifying one's chosen GP would likely be realized far into the future. Furthermore, patients often fail to fully exploit strategic opportunities even within the relatively simple current system. For example, it might be optimal for a patient to simultaneously switch to an open GP and join the waitlist for an even more preferred GP, which is allowed under the current mechanism. While there are instances of this type of behavior in the data, they are rare—simultaneous open-switches and waitlist joins occur in only 3 percent of patient-months in which a switch request was made.

Finally, we ignore the value of a long-term relationship with your GP. In principle, we could allow a patient's taste for their current GP to depend on the length of the relationship. However, our ability to credibly estimate this object is limited by the fact that we rarely observe the same patient switching multiple times after being assigned to different GPs. Our counterfactual simulations suggest that the rate of switch requests would change very little under alternative mechanisms, even though patients' specific GP choices would adjust in equilibrium. We therefore believe that our proposed mechanism design changes would have limited impact on patient-GP relationship capital.

## III.B Waiting Time Beliefs

Modeling beliefs is a key challenge in empirical market design, where market participants often do not have direct access to the information they need to understand the payoffs from different actions. In our setting, patients can easily observe the length of each GP's waitlist, but must infer how this would map into a waiting time. We propse a tractable model of beliefs that approximates the structure of a first-come, first-served queue in a way that depends on a small number of parameters that can be directly estimated from the data. Combined with the choice model, this belief model allows us to translate patients' observed responsiveness to waitlist lengths under the current system to similar responses under alternative mechanisms.

Beginning in waitlist position s, waiting time can be thought of as the sum of the time it takes to move from position s to position s-1; from s-1 to s-2; and so on up to the time from position 1 to being assigned. The time each step takes will depend on the rate at which slots become available on the GP's panel (through departures of incumbent enrollees), and the rate at which patients higher on the waitlist abandon it before being reassigned. Incumbent enrollees may depart their panel in the event of death, emigration, or a switch to another GP.

Patients standing on waitlists may abandon it in the event of death, emigration, or actively removing themselves from the waitlist.

We assume that patients perceive that slot vacancies and waitlist abandonments follow independent Poisson processes in continuous time. Each slot on GP j's panel becomes vacant at exponential rate  $\eta_j$ , and each patient waiting for GP j abandons the waitlist at exponential rate  $\kappa_j$ . If these processes are independent, then the time  $t_s$  it takes to move from position s to s-1 follows an exponential distribution with parameter  $N_j\eta_j + (s-1)\kappa_j$ , where  $N_j$  is GP j's panel cap. For a given patient,  $t_s$  and  $t_{s'}$  are independent for  $s \neq s'$ . A patient's expected total waiting time when entering GP j's waitlist at position w can then be written as

$$\mathbb{E}[T_j \mid w] = \mathbb{E}\left[\sum_{s=1}^w t_s\right] = \sum_{s=1}^w \frac{1}{N_j \eta_j + (s-1)\kappa_j},\tag{3}$$

and the expected discount factor as

$$\mathbb{E}\left[e^{-\rho T_j} \mid w\right] = \prod_{s=1}^{w} \frac{N_j \eta_j + (s-1)\kappa_j}{\rho + N_j \eta_j + (s-1)\kappa_j},$$
(4)

where equation Equation 4 is derived using the facts that the increments  $t_s$  are independent and exponentially distributed.

This belief model embeds two primary simplifications. First, it assumes assignments occur in continuous time at the moment vacancies become available. In practice, assignments are processed at the end of each month.<sup>29</sup> Second, it assumes that patients only consider the length of each waitlist in isolation when forming waiting time predictions. In principle, the fact that GP k's waitlist is unusually long—or that all nearby GPs have long waitlists—may predict how quickly GP j's waitlist will move. Given that in practice patients have limited information about the mapping from waitlist lengths to waiting times, we believe our belief model is a reasonable approximation.

<sup>&</sup>lt;sup>29</sup>In addition, at least 10 slots must be available before any patients are assigned from the waiting list. This is done to provide a buffer in case there are multiple births to patients already on the GP's panel.

## IV Estimation

## IV.A Sample and Parameterization

Geographic Subsample. For computational tractability, we estimate demand using a geographic and time-period subsample of our data. Geographically, we restrict to patients residing in the Trondelag region. Trondelag is attractive for this purpose because it is a populous region with a major population center (Trondheim), but the region boundaries are sparsely populated.<sup>30</sup> Its population accounts for about 8 percent of the country. In terms of time period, we focus on the 12 month period from December 2018 to November 2019, by which time GP waitlists were well-established. Appendix Table A.2 provides a comparison of key demographic characteristics between Trondelag and all of Norway over this period. Nothing about the two areas appears substantially different, with the exception that Trondelag is on average more rural.

In addition to geographic and time period restrictions, we also restrict patient choice sets. Our baseline choice set definition is a driving time radius of 60 minutes around a patient's municipality of residence.<sup>31</sup> Details about the construction of the demand estimation sample are provided in Appendix A.2. Our final demand estimation sample represents 4,213,049 patient-months (379,330 unique patients) and 457 unique GP panels.

**Parameterization.** We parameterize the attention and GP choice models as follows.

$$\lambda_{it} \stackrel{iid}{\sim} \text{Bernoulli}(p^{\lambda}(X_{it})) \tag{Attention}$$

$$v_{ijt} = -d_{ijt} + \delta_j + X_{ijt}\beta + \epsilon_{ijt} \mid \lambda_{it} = 1 \tag{GP choice}$$

$$\epsilon_{ijt} \stackrel{iid}{\sim} N\left(0, \sigma_{\epsilon}^2(X_{ijt})\right)$$

$$\rho_{it} = \rho \tag{Discount rate}$$

The attention shock  $\lambda_{it}$  is drawn independently each period according to a probability  $p^{\lambda}(X_{it})$  that depends on patient observables. Motivated by reduced form evidence in Appendix B.4, we include patient demographics (age, gender, permanent residency status), whether the patient

<sup>&</sup>lt;sup>30</sup> Of the 11 administrative regions (fylke) in Norway, Trondelag has the lowest outside-region GP enrollment. Only 1.7 percent of residents of Trondelag enroll with a GP outside of the region, compared to 7.7 percent of residents of the Oslo region. Appendix Figure A.4 provides a map of Norway and of Trondelag.

<sup>&</sup>lt;sup>31</sup>This definition is motivated by the fact that 97 percent of patients enroll with a GP within 60 minutes. Our estimates are not sensitive to adjusting the choice set definition between 45 and 90 minutes.

has recently or will imminently move, and if so, the distance of the move. An attentive patient  $(\lambda_{it} = 1)$  draws new taste shocks for each GP and makes a GP choice. Inattentive patients retain their taste shocks from the previous period. The flow payoff  $v_{ijt}$  from being assigned GP j depends on travel time  $d_{ijt}$  between patient i's municipality of residence and the GP's office; a GP fixed effect  $\delta_j$  capturing the common component of j's desirability, including any unobserved factors (Berry, Levinsohn and Pakes, 2004); interactions  $X_{ijt}\beta$  between patient and GP characteristics, capturing common components of patient-GP specific match value; and the idiosyncratic taste shock. Motivated by reduced-form evidence in Appendix B.2,  $X_{ijt}$  includes indicators for whether the patient and GP are of the same gender and same age, and we allow the value of age/gender homophily to vary across patient demographics. We allow the variance of the idiosyncratic taste shock to vary by patient age and residency status, in effect allowing variation in the distaste for travel time along these dimensions.

We normalize scale in the model by fixing patients' (dis)taste for travel time at -1. Travel time thus acts as a numeraire in the absence of prices, as is common in empirical market design applications (Abdulkadiroğlu, Agarwal and Pathak, 2017; Agarwal and Somaini, 2018). We normalize location by setting the fixed effect for one GP to zero. This leaves us with the following model parameters to estimate:  $\{\rho, \delta, \beta, \sigma_{\epsilon}, p^{\lambda}\}$ .

#### IV.B Estimation Procedure & Identification

We estimate the model in two steps. We first estimate the parameters governing the formation of patient beliefs using the empirical analogs of the objects described in section III.B. We then jointly recover the attention and preference parameters that best describe the observed data given our model and patient beliefs.

Waiting Time Beliefs. Consumers have concrete information about waitlist lengths and panel sizes, but have limited information about other factors. We therefore assume that  $(\eta_j, \kappa_j) = (\eta, \kappa)$  and estimate the latter on a per-month basis across all waitlist-month observations in our demand estimation sample. Out of 5,140 total GP panel-months considered (representing 457 unique GPs), 2,161 were panel-months in which the panel had a waitlist (representing 298 unique GPs). Among these panel-months, we then calculate the average

panel slot vacancy rate and the average waitlist abandonment rate, yielding belief parameters:

$$\eta = 0.0018$$
 (Panel slot vacancy rate)  
 $\kappa = 0.0170$  (Waitlist abandonment rate)

The average waitlist length over these months was 28, and the average panel cap was 1,084. Using our formula for expected waiting time (Equation 3), this panel cap and waitlist length coupled with our belief parameters would imply an expected waiting time of 12.8 months. For comparison, the average elapsed waiting time among patients on waitlists as of December 2019 was 7.9 months, which is a lower bound on the waiting time those patients ultimately experienced.

Attention and Preferences. We estimate the attention and GP choice model using Markov Chain Monte Carlo (MCMC) methods. We use a Gibbs' sampler with data augmentation to draw attention shocks  $\lambda_{it}$  and flow utilities  $v_{ijt}$  from their posterior distributions, and a Metropolis-Hastings step to update the discount rate  $\rho$  (McCulloch and Rossi, 1994; Gelman et al., 2013). We assume conjugate priors of  $(\delta, \beta) \sim N(\mu_0, \Sigma_0)$ ,  $p^{\lambda} \sim Beta(\alpha, \varphi)$ , and  $\sigma_{\epsilon}^2 \sim IW(\Psi_{\epsilon}^0, \nu_{\epsilon}^0)$ . The steps of the Gibbs' sampler can be written as follows for iteration b, where each step also conditions on patients' observable characteristics (Z) and choices (y):

(i) 
$$\delta_b, \beta_b \mid \mathbf{v}_{b-1}, \sigma^2_{\epsilon, b-1}, \mu_0, \Sigma_0$$

(ii) 
$$\sigma_{\epsilon,b}^2 \mid \mathbf{v}_{b-1}, \delta_b, \beta_b, \Psi_{\epsilon}^0, \nu_{\epsilon}^0$$

(iii) 
$$\rho_b \mid \delta_b, \beta_b, \sigma_{\epsilon,b}^2, y, Z$$

(iv) 
$$\lambda_b \mid p_{b-1}^{\lambda}, \delta_b, \beta_b, \sigma_{\epsilon,b}^2, y, Z$$

(v) 
$$p_b^{\lambda} \mid \lambda_b, \alpha, \varphi$$

(vi) 
$$\mathbf{v}_b \mid \lambda_b, \delta_b, \beta_b, \sigma_{\epsilon,b}^2, \rho_b, y, Z$$

Appendix C provides additional details on the updating steps. Though our estimator is Bayesian, it is asymptotically equivalent to maximum likelihood estimation (see, e.g., Van der Vaart 2000, Theorem 10.1, Bernstein von Mises) and computationally less demanding.<sup>32</sup> We interpret the posterior means and standard deviations in a frequentist manner for the purposes of inference.

<sup>&</sup>lt;sup>32</sup>Because discounting is multiplicative, the full likelihood would not have a tractable closed-form even if we assumed  $\epsilon$  was distributed Type-1 Extreme Value.

**Identification.** We can think of identification in three steps: identifying (i) the distribution of flow payoffs, (ii) the discount rate, and (iii) the attention parameters. Beliefs are assumed known.

First, suppose the discount rate  $\rho$  is known and attention is observed. The distribution of flow payoffs is non-parametrically identified by variation in travel time between patients' residences and GP offices. This argument treats travel time as a special regressor (Berry and Haile, 2014; Agarwal and Somaini, 2018) and requires that unobserved determinants of preferences for GPs are uncorrelated with patients' proximity to GP offices, conditional on observables. The key economic assumptions are that patients do not choose where to live based on access to primary healthcare, and that GPs do not locate their offices close to where patients live who particularly value seeing those GPs. We believe this is plausible in our context.

Second, given the distribution of flow payoffs, the discount rate is identified by the sensitivity of patients' choices to waitlist lengths (Waldinger, 2021).<sup>33</sup> A key identification challenge is that more desirable GPs will tend to have longer waitlists. However, because panel vacancies and waitlist departures are stochastic events, queue lengths naturally fluctuate due to events outside the control of a patient considering switching. This generates exogenous variation in the relative waitlist lengths of different GPs for patients who consider switching GPs at different times. A key identifying assumption is that patients do not time when they request to switch based on the waitlist lengths of specific GPs. In a first-come fist-served queue, when there is no direct cost of standing on a waitlist, there is no benefit to delaying a switch request until a patient's desired GP's queue is unusually short. We therefore view this threat as unlikely. It is also possible that a component of GP desirability is time-varying, so that a GP's waitlist tends to grow when the GP becomes more desirable. To the extent that this occurs, it would lead us to underestimate the discount rate.

Finally, the attention parameters are separately identified by attention shifters that are uncorrelated with preferences for specific GPs. In the ideal experiment, imagine a group of patients who pay attention with probability one (Abaluck and Adams-Prassl, 2021). If their preferences are drawn from the same distribution as the general population, their choices identify the other model parameters. We can then recover attention probabilities for the remaining patients by comparing their frequencies of switch requests and GP choices to those

<sup>&</sup>lt;sup>33</sup>Though we estimate a common discount rate for all patients, one could allow it to depend on observed characteristics. In practice, it was difficult to obtain precise estimates of  $\rho$  for different subgroups, and we could not reject that our point estimates were the same among subgroups in the specifications we tried.

of always-attentive patients. In the data, we observe that patients who move a long distance are much more likely to request to switch GPs than patients who move shorter distances or stay put. Our identifying assumption is that conditional on other observables, the distribution of GP preferences is uncorrelated with when or how far patients move. In practice, some patients wait years to switch GPs even after a long move, so we rely on parametric assumptions to jointly estimate patients' preferences and attention probabilities.

#### IV.C Estimates

We estimate three specifications. All specifications allow attention probabilities to differ flexibly by patient age, gender, and whether the patient is about to or recently moved. The first specification limits flow payoffs to depend only on distance and interactions between patient and GP age and gender. The second specification adds GP fixed effects, and the third specification allows the standard deviation of the idiosyncratic taste shock to vary by patient age and permanent residency status. All specifications estimate a common monthly discount rate  $\rho$ , reported as an annual rate.

Table 3 presents the parameter estimates. Column (1) estimates considerable sensitivity to waiting time, with an annual discount factor slightly below 0.95. When GP fixed effects are added in columns (2) and (3), this value falls to between 0.90 and 0.91, reflecting the fact that more desirable GPs have longer waitlists. As in the reduced form analysis, we estimate considerable homophily by gender and age. Based on estimates in column (1), a female patient under age 45 would travel 7.3 minutes farther than a male patient under 45 to see a female GP (6.3 minutes for a female/male patient over 45). Patients under 45 would travel about one minute farther than a patients over 45 to see a GP under 45. Adding GP fixed effects and heterogeneity in the variance of the taste shock to the model leaves the estimates of age and gender homophily nearly unchanged.

Column (3) allows the variance of the idiosyncratic taste shock to vary by patient age and residency status, which can be equivalently thought of as allowing for heterogeneity in the distaste for travel time relative to idiosyncratic factors. We find that the distaste for travel time is considerably higher for older permanent residents than for other patients. In both columns (2) and (3), we estimate considerable variation in overall GP desirability as well as in the value of the idiosyncratic taste shock. Column (2) estimates a standard deviation of GP fixed effects of 31 minutes, and a standard deviation of idiosyncratic shock of 12.6 minutes. In column (3), the standard deviation of GP fixed effects falls to between 16 and 24 minutes,

Table 3. Preference Parameter Estimates

	(1)		(2)		(3)	(3)	
Variable	β	SE	β	SE	$\beta$	SE	
Annual Discount Factor	0.944	0.002	0.904	0.007	0.908	0.007	
Travel time (minutes) $^{\dagger}$	-1.000		-1.000		-1.000		
S.D. GP Fixed Effects			31.008	4.962			
S.D. GP Fixed Effects, Temp. res.					23.092	1.776	
S.D. GP Fixed Effects, Perm. res. age $\leq 45$					24.195	1.722	
S.D. GP Fixed Effects, Perm. res. age $> 45$					16.400	1.264	
Male GP	-3.036	0.365					
$\times$ Perm. res. female, age 16–45	-1.300	0.414	-2.448	1.051	-2.886	0.425	
$\times$ Perm. res. female, age 45+	-0.608	0.424	-0.922	1.014	-1.170	0.477	
$\times$ Perm. res. male, age 16–45	5.986	0.421	4.967	0.997	4.054	0.474	
$\times$ Perm. res. male, age 45+	5.754	0.477	5.947	1.018	2.761	0.686	
GP age 45+	-2.184	0.404					
$\times$ Perm. res. female, age 16–45	-0.446	0.441	-0.821	1.090	-1.787	0.394	
$\times$ Perm. res. female, age 45+	0.499	0.440	0.330	1.053	-0.583	0.482	
$\times$ Perm. res. male, age 16–45	-0.404	0.460	-0.309	1.071	-1.496	0.424	
$\times$ Perm. res. male, age 45+	0.267	0.558	0.937	1.069	-0.713	0.632	
S.D. idiosyncratic shock	14.885	0.161	12.643	0.334			
S.D. idiosyncratic shock, Temp. res.					12.296	0.314	
S.D. idiosyncratic shock, Perm. res. age $\leq 45$					12.894	0.470	
S.D. idiosyncratic shock, Perm. res. age $> 45$					8.738	0.378	

Notes: The table reports parameter estimates from the GP choice model described in Section IV. We simulate 40,000 draws from the Markov chain and drop the first 20,000 for each specification. The table reports the mean and standard deviation of the remaining draws as the point estimate and standard error of each parameter (respectively). Columns (2) and (3) include a fixed effect for each GP, with one normalized to zero. Column (3) allows the standard deviation of the idiosyncratic shock to differ by residency status and age. †By normalization

and the standard deviation of idiosyncratic shock falls to between 9 and 12 minutes.<sup>34</sup>

Table 4 presents parameter estimates for the attention model. Estimates are very similar across specifications, so we focus on column (3). Our estimates imply that non-movers consider switching GPs far less often than patients who have recently moved, consistent with observed switching patterns (c.f. Table 1). Among non-movers, temporary residents pay attention most often—1.084 percent chance per month (approximately once every 7.5 years)—while older men consider switching just once every 25 years.

<sup>&</sup>lt;sup>34</sup>Variance in the idiosyncratic shock may in part reflect the fact that we observe only a patient's municipality of residence rather than their exact address, introducing measurement error in travel time. Using data from an earlier time period in which we had exact address, we investigated whether measurement error in travel time from observing municipality rather than exact address is correlated with other patient characteristics, and found essentially no relationship.

Table 4. Monthly Attention Probability Estimates

	(1)		(2)		(3)	(3)	
Variable	$p^{\lambda}$	SE	$p^{\lambda}$	SE	$p^{\lambda}$	SE	
No Recent or Imminent Move						_	
$\times$ Temporary resident	1.21	0.02	1.33	0.02	1.08	0.02	
$\times$ Perm. res. female, age $\leq 45$	0.75	0.01	0.85	0.01	0.82	0.02	
$\times$ Perm. res. female, age $> 45$	0.47	0.01	0.47	0.01	0.47	0.01	
$\times$ Perm. res. male, age $\leq 45$	0.44	0.01	0.44	0.01	0.48	0.03	
$\times$ Perm. res. male, age $>45$	0.28	0.01	0.28	0.01	0.33	0.01	
$Moved \leq 30 minutes, this or next month$							
× Temporary resident	6.92	1.13	6.86	1.13	6.93	1.13	
× Perm. res. female	4.63	0.38	4.63	0.37	4.63	0.39	
$\times$ Perm. res. male	3.35	0.33	3.35	0.33	3.35	0.33	
$Moved \leq 30 minutes, prev. 6 months$							
× Temporary resident	3.43	0.55	3.42	0.55	3.41	0.57	
× Perm. res. female	2.44	0.18	2.45	0.18	2.45	0.17	
$\times$ Perm. res. male	5.99	0.27	1.71	0.15	1.71	0.15	
Moved >30 minutes, this or next month							
× Temporary resident	18.50	2.27	18.51	2.26	18.59	2.32	
× Perm. res. female	8.85	0.67	8.84	0.66	8.83	0.65	
$\times$ Perm. res. male	6.86	0.59	6.82	0.58	6.84	0.61	
Moved >30 minutes, prev. 6 months							
× Temporary resident	7.28	1.13	7.33	1.17	7.28	1.12	
× Perm. res. female	3.83	0.28	3.82	0.28	3.83	0.29	
$\times$ Perm. res. male	2.86	0.24	2.85	0.24	2.85	0.24	

Notes: The table reports parameter estimates from the attention model. Parameters represent the probability a patient is attentive in a given month, reported in percentage points. These parameters are estimated jointly with the preference parameters reported in Table 3. The categories are mutually exclusive and exhaustive. A patient has No Recent or Imminent Move if they did not change their municipality of residence in the six months prior to or one month after the current month. After a patient has been attentive during a given move spell, they are treated as a non-mover during the rest of that move spell.

Patients who have moved consider switching an order of magnitude more often. We estimate separate attention probabilities for short and long moves, where short means less than 30 minutes' drive time between origin and destination municipality, and long means over 30 minutes. We also allow attention to differ by whether the move is imminent (occurring this month or next month) or recent (in the past 6 months), reflecting the fact that we see a large immediate impact of moving on the probability of switching GPs in the data (c.f. Appendix Table B.2). Finally, we allow mover attention to depend on gender and residency status. Movers exhibit stark differences in attention probabilities along all three dimensions. Patients are most attentive in the month prior to or of a move. A temporary resident moving over 30 minutes this or next month has an 18.59 percent chance of considering switching GPs. The

probability remains high, but falls to 7 percent per month in the six months following the move. Permanent residents exhibit a similar pattern, but with lower attention probabilities. Distance of move is also highly predictive. A female permanent resident moving less than 30 minutes has only a 22 percent cumulative attention probability in the 8 months around that move. If the move were over 30 minutes, this rises to 34 percent. Attention around move events will be important for counterfactual simulations, because patients are most attentive when they are also most mismatched with their current GP.

## V Counterfactual Simulations and Welfare

We now use our estimates to predict equilibrium assignments under alternative waitlists mechanisms. Section V.A describes the simulated dynamic economy. Section V.B then formally defines our counterfactual mechanisms of interest, Section V.C defines an equilibrium, and Section V.D presents the results.

### V.A Simulated Dynamic Economy

We consider an economy with a finite set of patients (agents) and GPs (objects). The set of patients is given by  $I = \{i_1, ..., i_n\}$ . Patients have types  $x \in \mathcal{X}$ . The set of GPs is given by  $J = \{j_1, ..., j_m\}$ . GPs have types  $z \in \mathcal{Z}$ . We treat  $\mathcal{X}$  and  $\mathcal{Z}$  as finite sets. An allocation  $\mu: I \to J$  is a many-to-one mapping of patients to GPs, such that each patient is assigned to exactly one GP.

GP types include age, gender, office location, and panel cap size. All GP characteristics are fixed over time. Patient types include demographics and location of residence. There are five possible demographic types: {Perm. res. female  $\leq 45$ , Perm. res. female > 45, Perm. res. male > 45, Perm. res. male > 45, Temp. res.}, and 45 possible locations of residence (municipalities in the Trondelag region). The combination of patient municipality and GP office location pin down a travel time between every patient type and every GP.

Patient characteristics evolve over time according to a stationary Markov process M:  $\mathcal{X} \to \mathcal{X}$ . Patients also have a chance of dying, in which case they immediately experience a "rebirth" in which they are removed from their current GP and reassigned to the current GP of a randomly selected young woman living in their same location of residence. The simulation therefore allows for panel vacancies to arise naturally but, given the standard

practice of enrolling babies with their mother's GP, less frequently on GP panels with many young women.

We initialize the set of patients and GPs in the economy based on the distribution of patient and GP types observed in the Trondelag region in December 2019. We calibrate the patient type transition process M based on type transitions observed in Trondelag over the period 2017–2019. Appendix Table D.1 provides summary statistics on the set of patients and GPs in the simulated economy. Appendix D.1 provides additional details on the construction of our initial conditions as well as on the transition process M.

#### **Simulation Procedure.** In each period, the following steps occur (in order):

- 1. (*Demographic transitions*) Patients draw a new type and a death shock. Patients that die are removed from their current GP panel as well as any waitlists they are on, and added to the GP panel of the mother to whom they are reborn.
- 2. (Attention) Patients draw attention shocks according to the probabilities  $p^{\lambda}(x)$  estimated in Table 4.
- 3. (*GP Choice*) Attentive patients sequentially arrive to the mechanism. Upon entry, they consider all GPs, draw new preferences  $(\epsilon_{ij})$ , formulate flow indirect utilities for each GP  $(v_{ij})$  (based on parameter estimates in Table 3), and report their GP request(s) to the mechanism. Patients who request to stay with their current GP or switch to an open GP are immediately reassigned and exit the mechanism. Patients who request a full GP are placed on the waitlist.
- 4. (*Matching Algorithm*) The patient-GP matching algorithm is executed. Patients that are successfully reassigned exit the mechanism. All other patients remain there until the following period.

Realizations of the demographic transition process, the receipt of attention shocks, and draws of idiosyncratic preferences are held fixed across simulations of alternative mechanisms. Appendix Table A.3 summarizes these realizations.

#### V.B Allocation Mechanisms

Let  $\mu_0$  be the allocation at the start of a given period. Each GP j has capacity  $N_j$ , a set of currently enrolled patients  $\mu_0^{-1}(j)$ , and a set of patients  $w_j$  on their waitlist. Each patient

on a waitlist has waited a length of time  $t_i$ . Let  $\succ_j$  denote GP j's (strict) preferences over patients, which encode the priority rules of the mechanism. Under a **first-come**, **first-served** (**FCFS**) priority rule, patients that have waited longer have higher priority:  $\forall l, k \notin \mu_0^{-1}(j)$  and  $\forall l, k \in \mu_0^{-1}(j), l \succ_j k$  iff  $t_l > t_k$ . Under a priority rule that **respects endowments**, incumbent patients always have higher priority than non-incumbent patients at their current GP:  $\forall l, k \in I, k \succ_j l$  if  $k \in \mu_0^{-1}(j)$  and  $l \notin \mu_0^{-1}(j)$ . All priority rules we consider will respect endowments.

An attentive patient's GP request takes the form of a rank-order preference list (ROL)  $R_i$ . In all of our mechanisms of interest, patients may join at most one waitlist, so  $R_i$  has length at most two. The requested (waitlist) GP is ranked first, and the current GP is ranked second. A matching algorithm  $\phi$  maps a set of patient-reported ROLs  $\mathbf{R}$ , GP priorities  $\succ$ , and panel caps  $\mathbf{N}$  into an allocation  $\mu$ . An allocation mechanism is defined as the triplet  $[\mathbf{N}, \succ, \phi]$ , in combination with rules regarding the maximum length of patients' ROLs and how often the matching algorithm is run. Our counterfactuals change both the priority rule  $\succ$  and the matching algorithm  $\phi$  applied each period. Patients' reported ROLs respond endogenously to these changes.

While the matching algorithm is run only periodically (once per month), an allocation mechanism operates in continuous time. Attentive patients arrive continuously and submit ROLs. They then remain in the mechanism until they can be successfully reassigned (or they die). If they receive a subsequent attention shock while still in the mechanism, they have the option to change their ROL (switch waitlists), resetting their wait time priority. So long as GP priorities respect endowments, priority increases with waiting time, and patients can include their current GP at the end of their ROL, it is ex-post individually rational for attentive patients to participate in the mechanism.

We consider three primary counterfactual allocation mechanisms, in addition to the status quo mechanism. First, we run the TTC algorithm on top of Norway's existing waitlists algorithm, just as in the mechanical simulations from Section B.1, but where we can now endogenize patient responses. We then consider two alternatives intended to address the distributional and fairness concerns that—as we saw in the naive simulations—may arise under TTC. Each of these mechanisms is described below.

Waitlists. This is the allocation mechanism currently used in Norway. Priorities are FCFS. The matching algorithm used is the following:

Step 1: For each GP j, let  $O_j = N_j - |\mu_0^{-1}(j)|$  be the number of open slots on j's panel.

Assign the  $O_j$  highest-priority patients on j's waitlist to j's panel; remove each of these patients from their current GP's panel and from the waitlist.

Step k: Repeat Step 1 for the panels and waitlists resulting from Step k-1.

The algorithm terminates if no patients are reassigned in a step. When this occurs, there are no patients waiting for GPs with open slots.

Waitlists with Top-Trading Cycles (TTC). This is our main proposal for Norway's GP allocation system. Priorities are still FCFS. The matching algorithm first runs the Waitlists algorithm (as above), and then runs the TTC algorithm. The TTC algorithm works as follows. Each GP begins with pseudo-capacity  $\tilde{N}_j$  equal to their number of open panel slots plus the number of their current patients who are currently in the mechanism hoping to switch away to another GP.

Step 1: Each patient "points to" their preferred GP according to  $R_i$ , and each GP points to their preferred patient according to  $\succ_j$ . There is at least one cycle, i.e., an ordered list  $\{i_1, j_1, i_2, j_2, ..., i_k, j_k\}$  where  $i_1$  points to  $j_1$ ,  $j_1$ , points to  $i_2$ , ..., and  $j_k$  points to  $i_1$ . Further, each patient and GP can be part of at most one cycle. Each patient in a cycle is assigned to the GP they point to and is removed from their current GP's panel and the algorithm. Each GP in a cycle has their pseudo-capacity reduced by one, and is removed from the algorithm when their pseudo-capacity falls to zero.

Step k: Repeat Step 1 with the remaining patients and updated GP pseudo-capacities from the end of Step k-1.

The algorithm terminates when no patients remain in the algorithm.

Waitlists with Top-Trading Cycles and Priority (TTCP). This mechanism is identical to TTC, but modifies priorities so that patients with undersubscribed GPs are prioritized above patients with oversubscribed GPs (while still respecting endowments). Formally,  $\forall l, k \notin \mu_0^{-1}(j), l \succ_j k$  if l currently has an undersubscribed GP and k currently has an oversubscribed GP. Among patients with the same over/undersubscribed status, there is FCFS priority. We classify a patient's current GP as over/undersubscribed at the moment they enter the mechanism.<sup>35</sup> A GP is undersubscribed if it has at least one open slot on its panel.

TTCP attempts to address some of the adverse distributional consequences from introducing

<sup>&</sup>lt;sup>35</sup>While it is possible that a GP could transition to/from being over/undersubscribed while their patient remains in the mechanism, these transitions rarely occurred in our simulations, and modeling patient beliefs about this possibility would be highly complex.

TTC, while preserving its benefits. Rather than preventing waiting patients from exchanging their GPs, TTCP gives patients who are unlikely to benefit from cycles priority for other vacancies.

Waitlists with Deferred Acceptance (DA). This mechanism is identical to Waitlists, but replaces the matching algorithm used with the patient-proposing deferred acceptance (DA) algorithm. Again, let  $\tilde{N}_j$  denote GP j's pseudo-capacity. The DA algorithm proceeds as follows:

Step 1: Each patient "proposes to" their preferred GP according to  $R_i$ . Each GP j provisionally accepts proposals from its  $\tilde{N}_j$  most preferred patients according to  $\succ_j$  and rejects any remaining proposals.

Step k: Any patients who were rejected in the previous round propose to their mostpreferred GP (according to  $R_i$ ) who has not yet rejected them. Each GP j provisionally accepts proposals from its  $\tilde{N}_j$  most preferred patients according to  $\succ_j$  and rejects any remaining proposals.

The algorithm terminates when no patient is rejected.

Relative to Waitlists, the key advantage of DA is to allow trades among patients at the front of their respective waitlists. Relative to TTC, however, an attractive property of DA is that, like Waitlists, it strictly respects FCFS waiting time priority. No patient may "jump" to the front of the queue and be reassigned to a GP for whom another patient was waiting longer. This idea reflects DA's well-known property of stability (Gale and Shapley, 1962), which is also known as elimination of justified envy (Abdulkadiroğlu and Sönmez, 2003). Further, because patient-proposing DA yields the patient-optimal stable match with respect to reported preferences, it represents the best any algorithm in this class can do without violating FCFS priority (i.e., generating envy). Nevertheless, by strictly respecting waiting time priority, DA may substantially limit trading opportunities relative to TTC.

## V.C Beliefs, Decisions, and Equilibrium

In all of our counterfactuals, attentive patients choose a GP by solving the choice problem in Equation (2):

$$\max_{j \in \mathcal{J}_{it}} \mathbb{E}\left[e^{-\rho T_{ij}} \mid \mathbf{w}_{it}\right] \left(v_{ijt} - v_{ij_0t}\right).$$

Counterfactual mechanisms will not only change the number of patients on the waitlist at a given time  $\mathbf{w}_{it}$ , but also patients' beliefs about the speed with which waitlists move, i.e., the expected discount factor function  $\mathbb{E}\left[e^{-\rho T_{ij}} \mid \mathbf{w}_{it}\right]$ . How these beliefs adjust will determine patients' equilibrium responses to alternative mechanisms. To accommodate the additional complexity of TTC, we must adapt the belief model from Section III.B.

As before, patients have beliefs about how quickly a waitlist moves from the front  $(\eta)$ , and how often waiting patients depart the waitlist before reaching the top  $(\kappa)$ . Under TTC, beliefs must also account for the fact that a patient can be successfully reassigned before reaching the top of the waitlist if they participate in a cycle. Further, patients ahead in the queue may depart because they are assigned through a cycle, as well as due to exogenous departures.

We modify the belief structure as follows. In each position s, a patient will either (i) move to position s-1 due to a waitlist departure or assignment from the front of the queue, or (ii) be reassigned through a cycle. We assume that these two events are perceived to follow independent, memoryless arrival processes. We allow the rate of being assigned through a cycle  $\chi_{j_0s}$  to depend on a patient's position s as well as on whether their current GP  $j_0$  is undersubscribed.<sup>36</sup> Patients are assigned from the top of GP j's waitlist at rate  $N_j\eta$ . Each patient on the waitlist departs at rate  $\kappa$ , which now includes both abandonments and reassignments through a cycle. A patient's expected discount factor when entering GP j's waitlist at position s can now be written

$$\mathbb{E}[e^{-\rho T_{ij}} \mid j_0, s] = \frac{m_{js} + \chi_{j_0s}}{\rho + m_{js} + \chi_{j_0s}} \left( \frac{\chi_{j_0s}}{m_{js} + \chi_{j_0s}} + \frac{m_{js}}{m_{js} + \chi_{j_0s}} \mathbb{E}[e^{-\rho T_{ij}} \mid j_0, s - 1] \right)$$

$$= \frac{\chi_{j_0s}}{\rho + m_{js} + \chi_{j_0s}} + \frac{m_{js}}{\rho + m_{js} + \chi_{j_0s}} \mathbb{E}[e^{-\rho T_{ij}} \mid j_0, s - 1], \qquad (5)$$

where  $m_{js} \equiv N_j \eta + (s-1)\kappa$  is the rate at which the patient moves forward in the queue.<sup>37</sup> Equation 5 provides a recursive formula for the expected discount factor at any position s. We parameterize  $\chi_{jos}$  such that it equals zero for patients with an undersubscribed GP (who

<sup>&</sup>lt;sup>36</sup>In principle,  $\chi_{j_0s}$  could depend in a complex way on the state of the mechanism, including the lengths of all GP waitlists and number of open slots on each GP's panel, as well as the GP the patient has requested. Our simplification strikes a balance between capturing the most important determinants of waiting times and having low complexity.

<sup>&</sup>lt;sup>37</sup>The intuition behind this formula is as follows. The next event that occurs is either participating in a cycle or moving one position forward in the queue. If these two processes are independent and memoryless, then the next event occurs at exponential rate  $m_{js} + \chi_{j_0s}$ . The ratio  $\frac{m_{js} + \chi_{j_0s}}{\rho + m_{js} + \chi_{j_0s}}$  is the expected discount factor for the time of that event. Given that an event occurs, it is participating in a cycle with probability  $\frac{\chi_{j_0s}}{\chi_{j_0s} + m_{js}}$ , in which case assignment is immediate and the subsequent discount factor is 1. The probability the event is moving up a position is  $\frac{m_{js}}{\chi_{j_0s} + m_{js}}$ , and the subsequent discount is simply  $\mathbb{E}[e^{-\rho T_{ij}} \mid j_0, s-1]$ .

have no chance of participating in a cycle), and is log-linearly related to waitlist position-relative-to-panel cap for patients with an oversubscribed GP:  $\chi_{j_0s} = \mathbb{1}[j_0 \text{ oversub.}] \exp(\chi_0 + \chi_1 \log(s/N))$ . Note that if  $\chi_{j_0s}$  is restricted to zero for all patients, this formulation of beliefs collapses to the original beliefs structure relevant for Waitlists and DA.

We compute counterfactual equilibria in which belief parameters are consistent with the waiting times implied by patients' optimal decisions. Appendix D.2 describes our procedure in detail. The algorithm iteratively updates patients' optimal decisions given the state of the simulation algorithm and the belief parameters implied by the simulation, until the belief parameters (and hence decisions) converge. Appendix Table D.2 reports equilibrium beliefs.

#### V.D Results

Table 5 reports equilibrium outcomes under our primary mechanisms of interest. It also reports outcomes under a benchmark simulation, **No Caps**, in which GP panel caps (and thus all scarcity in the economy) are removed. This benchmark provides an upper bound on the welfare that can be achieved by any mechanism within our framework.<sup>39</sup> We report outcomes from a 5-year window at the end of out simulation period, when the economy has reached a stationary equilibrium.

In the long-run stationary equilibrium of Norway's current mechanism (Waitlists), 9.4 percent of patients are on a waitlist, and 82.2 percent of GPs have a waitlist. Patients' expected waiting time to switch to the average GP (including zeros for those without waitlists) would be 16.7 months. Each month, an average of 2,299 patients receive attention shocks and consider switching GPs (c.f. Appendix Table A.3). Among these patients, 85.2 percent choose to join a waitlist, while the rest choose a GP with open slots or to remain with their current GP. The average attentive patient expects to successfully obtain their chosen GP after 16.8 months.<sup>40</sup> Despite considerable sensitivity to waiting time, many patients are willing to wait for their

<sup>&</sup>lt;sup>38</sup>In the TTCP mechanism, we allow patients with undersubscribed GPs to have different beliefs about  $\kappa$ , since any patients ahead of them on a waitlist will also have undersubscribed GPs and thus have no chance of departing the waitlist by participating in a cycle.

<sup>&</sup>lt;sup>39</sup>Of course, allowing GP panel sizes to grow arbitrarily would in reality likely reduce the value of highly-demanded GPs, for example by increasing waiting time for appointment. The advantage of this infeasible benchmark is that it is straightforward to compute. In contrast, the first- or second-best allocation would require solving a high-dimensional dynamic optimization problem that accounts for future (stochastic) arrivals as well as all current patients' preferences and all GPs' availability.

<sup>&</sup>lt;sup>40</sup>Relative to our data, these longer equilibrium waiting times reflect the fact that the waitlists were still growing rapidly during our sample period.

Table 5. Outcomes under Alternative Mechanisms

	Waitlists	TTC	DA	TTCP	No Caps
GP waitlists					
Pct. of population on a waitlist	9.4	8.9	9.3	9.6	_
Pct. of GPs with a waitlist	82.2	78.3	82.1	79.3	_
Mean E(waittime)   curr. GP undersub.	16.7	22.8	16.7	18.9	_
curr. GP oversub.	16.7	10.7	16.7	12.2	_
Attentive patient choices					
Mean E(waittime) at chosen GP	16.8	14.1	16.8	15.2	_
Pct. waitlist joins	85.2	84.6	85.2	85.1	_
curr. GP undersub.	79.0	74.8	79.1	77.2	_
curr. GP oversub.	86.2	86.3	86.1	86.3	_
True pref. rank of chosen GP	1.79	1.63	1.78	1.63	1.00
curr. GP undersub.	1.94	2.29	1.93	2.04	1.00
curr. GP oversub.	1.76	1.52	1.76	1.56	1.00
Realized assignments					
Travel time to current GP, mean (med.)	17.3 (6.5)	16.9 (6.4)	17.3 (6.5)	17.1 (6.4)	16.8 ( 6.4)
Pct. with same gender GP   young female	59.3	60.3	59.3	60.3	68.7
young male	61.8	61.2	61.9	61.1	52.6
Welfare					
Flow payoff from current GP, mean (med.)	_†	0.75(0.69)	0.01(0.01)	0.46(0.45)	5.34 (4.53)
Perpituity equiv. of GP choice, mean (med.)	_†	1.25 (0.83)	0.01 (0.00)	1.08 (0.54)	6.15 (4.21)

Notes: The table reports statistics on outcomes generated in months 392–451 of the simulation, out of 500 total months. Statistics are first computed within month and then averaged across simulation months. E(waittime) is the expected waiting time implied by patient's equilibrium beliefs and current waitlist lengths. True pref. rank of requested GP is the rank of a patient's requested GP in their true flow payoff ordering. †By normalization.

first choice GP. The average rank of a patient's requested GP in their true preference list is 1.79.

To quantify the gains from introducing TTC, we measure welfare in two different ways. First, we calculate the flow payoff experienced by every patient in the economy each period. This measure would be relevant to the utilitarian policymaker interested in maximizing the present discounted value of all future payoffs in the economy. It also has the advantage that it relies only on realized assignments. However, in a dynamic economy, a patient's current GP at any given time may differ across mechanisms for two reasons: (i) due to GP switching events (attention spells) that occurred earlier in time, and (ii) due to contemporaneous differences in the ease with which an attentive patient can switch GPs due to changes in equilibrium waiting times. To highlight the latter channel, we introduce an alternative welfare measure that isolates the value of switching opportunities. Specifically, we measure the net present value (NPV) of an attentive patient's choice problem, holding the patient's current

GP fixed.<sup>41</sup> We then multiply by patients' discount rate  $\rho$  (estimated to be 0.0081), yielding the perceived perpetuity flow payoff associated with attentive patients' optimal choice under each mechanism. This measure highlights the gains for patients precisely when they consider switching GPs. It also allows us to compare patient welfare as a function of characteristics that are endogenous to the mechanism, including whether the patient currently has an over-or undersubscribed GP. For both welfare measures, we normalize welfare under Waitlists to zero for all patients.

Relative to the status quo, introducing TTC reduces waiting times and increases patient welfare. The average attentive patient now successfully obtains their chosen GP after 14.1 months, and a smaller share of patients are on a waitlist at a given time. Measured by mean flow payoffs from realized assignments, patient welfare increases by the equivalent of 0.75 minutes' driving time. This improvement is significant in magnitude (more than 13 percent of the gains under the benchmark of No Caps). More than half is attributable directly to patients being matched with closer GPs (0.4 minutes), with the remainder driven by improved match quality on both observable and unobservable dimensions. The equivalent perpetuity payoff perceived by the average attentive patient is 1.25 minutes.<sup>42</sup> These average improvements are reflected in patients' behavioral responses; they are more likely to request their first-choice GP, with the mean flow payoff rank of their chosen GP falling to 1.63.

Distributional Implications. Table 6 summarizes welfare outcomes (using the NPV measure) by subgroups of attentive patients. In terms of demographics, the welfare gains from TTC conditional on being attentive are concentrated among younger patients. Female patients also derive especially large benefits because they are more likely to be attentive than male patients. Patients who moved in the last 12 months also realize large benefits from TTC (2.3 minutes), reflecting the fact that TTC reduces waiting times and these patients tend to be highly mismatched with their current GP. However, patient moves are not the only dynamic driving patient-GP mismatch; patients who have never moved also benefit (1.0 minutes). In terms of geography, patients in both urban and rural areas benefit, but the gains are largest

<sup>&</sup>lt;sup>41</sup>Appendix D.3 provides additional details.

 $<sup>^{42}</sup>$ The difference between these numbers reflects two things. First, the NPV measure re-weights patient months relative to the flow payoff measure because it is calculated in *attentive* patient months only, and from there discounts future payoffs according to  $\rho$ . Since attentive patients are weakly improving their situation (relative to being inattentive), welfare gains tend to be larger according to the NPV measure than according to the flow payoff measure. Second, patients are over-optimistic about the flow of welfare gains they will receive over an infinite horizon because in reality they experience subsequent shocks (e.g., moving or dying), the probability of which they do not take into account at the moment of attention.

among rural patients (2.1 minutes), who tend to face the longest travel times and thus have the greatest potential for geographic mismatch. Finally, it is worth noting that for most groups, changes in median welfare are also positive and economically significant, suggesting that gains are widely spread rather than concentrated among a minority of patients.

Table 6. Distribution of Welfare Gains Relative to Waitlists

	Frac. of attn. pats.	TTC	DA	TTCP	No Caps
All attentive patient-months	1.00	1.3(0.8)	0.0(0.0)	1.1 (0.5)	6.1(4.2)
Patient demographics					
Perm res. male<45	0.19	1.4(1.0)	0.0(0.0)	1.2(0.6)	6.9(4.8)
Perm res. male≥45	0.16	1.0(0.6)	0.0(0)	0.9(0.3)	4.8(3.0)
Perm. res. female < 45	0.30	1.5(1.1)	0.0(0.0)	1.2(0.8)	7.1(5.3)
Perm. res. female≥45	0.22	0.9(0.6)	0.0(0)	0.8(0.4)	4.7(3.2)
Temporary resident	0.13	1.4(0.9)	0.0(0.0)	1.2(0.6)	6.9(4.8)
Months since move					
Moved in last year	0.13	2.3(1.1)	0.0(0)	2.1(0.7)	11.3(7.9)
Moved over a year ago	0.34	1.2(0.8)	0.0(0.0)	1.0(0.5)	6.2(4.3)
Never moved	0.53	1.0 (0.8)	0.0(0.0)	0.8(0.5)	4.8(3.6)
Geographic location					
Rural	0.19	2.1 (0.4)	0.0(0)	2.0(0.3)	8.0(3.6)
Suburban	0.36	1.0(0.7)	0.0(0.0)	0.8(0.4)	5.9(4.2)
Urban (Trondheim)	0.45	$1.1\ (1.0)$	0.0(0.0)	0.9(0.6)	5.5 (4.4)
$Current\ GP\ oversubscribed?$					
No	0.13	-0.8 (-0.4)	0.0(0)	0.0(0)	6.4(4.4)
Yes	0.87	1.6 (1.0)	0.0 (0.0)	1.2 (0.6)	6.1 (4.2)

Notes: This table compares the perceived value of the mean (median) attentive patient's optimal GP choice under each mechanism, relative to the status quo mechanism Waitlists. Value is reported in a perpetuity equivalent monthly flow payoff in terms of travel time minutes to GP. Statistics are averaged across all attentive patients in months 392–451 of the simulation, holding each patient's current GP fixed at their assignment under Waitlists. See Appendix D.3 for additional details.

Although TTC benefits the majority of patients, it has particularly uneven consequences along an important dimension—whether a patient's current GP is oversubscribed. Table 5 shows that while TTC reduces waiting times for the average GP by 6 months (from 16.7 to 10.7) for patients with oversubscribed GPs, it *increases* waiting times (from 16.7 to 22.8 months) for patients with undersubscribed GPs. Patients' GP choices reflect the disparity along this dimension. Patients with undersubscribed GPs become less selective under TTC, choosing GPs with an average preference rank of 2.29 (instead of 1.94 under Waitlists), and joining waitlists less frequently. Patients with oversubscribed GPs, on the other hand, become more selective, choosing better-matched GPs and becoming more likely to join a waitlist.

These differences in waiting times and behavioral responses are reflected in patient welfare.

Table 6 reports that attentive patients with an undersubscribed GP are substantially worse off under TTC—the perpetuity equivalent of 0.8 minutes' travel time. Although these harms are offset by larger gains for patients with oversubscribed GPs, they may raise equity concerns for policymakers. In particular, it may seem unfair to disadvantage patients who already have a less desirable GP. This motivates exploring alternative mechanisms that attempt to improve outcomes for this group of patients.

Addressing Harms using DA and TTCP. The third column of Table 5 shows that DA achieves essentially no improvement over the status quo mechanism. Recall that DA does not execute trades that violate FCFS priority; patients may only swap GPs if all patients in front of them on their respective waitlists are also reassigned that month. As a result, DA reassigns few patients earlier than under Waitlists, and since those patients are already near the front of the queue, their waiting time reduction is small. This finding demonstrates a fundamental trade-off between eliminating envy—here, not allowing patients to "cut" in line—and finding additional gains from trade.<sup>43</sup>

In contrast to DA, TTCP attempts to improve outcomes for patients with undersubscribed GPs without preventing feasible trades. This is done by prioritizing patients with undersubscribed GPs above those with oversubscribed GPs, in effect ensuring that vacant slots are first offered to patients unlikely to benefit from cycles. The fourth column of Table 5 shows that TTCP achieves the majority of the welfare gains of TTC (0.46 vs 0.75 minutes in terms of the flow payoff measure; 1.08 vs 1.25 in terms of the NPV measure). Compared to TTC, more patients are standing on a waitlist at a given time, and patients expect to wait 1.1 months longer at their chosen GPs. For a patient with an oversubscribed GP, the expected waiting time for the average GP in their choice set rises from 10.7 to 12.2 months. However, this is offset by a much larger drop in expected waiting times for patients with undersubscribed GPs, from 22.8 to 18.9 months. These patients become more selective, requesting a GP with an average preference rank of 2.04 instead of 2.29, while patients with oversubscribed GPs become only slightly less selective.

One reason why TTCP yields smaller welfare gains than TTC is that prioritizing patients with undersubscribed GPs may reduce the total number of switches. When a patient with an undersubscribed GP is reassigned, the slot they vacate on their current GP's panel is unlikely to be demanded by another patient. Thus, the "chain" created by their assignment

<sup>&</sup>lt;sup>43</sup>The result that DA heavily restrict gains from trade mirrors empirical findings in other studies, e.g., Combe et al. (2022).

to a vacancy is short. Rather than facilitating more assignments, as would often occur under TTC, assignments to a vacancy under TTCP usually end with the assigned patient. Indeed, the rate at which the waitlist moves from the front is 30 percent lower under TTCP than under TTC (c.f. Appendix Table D.2). Patients with undersubscribed GPs still benefit because they are placed higher on the waitlist, but the waitlists move more slowly overall.

Despite yielding smaller improvements than TTC, the results from TTCP are encouraging for policymakers concerned about the distributional consequences of introducing TTC in a market where some patients have more desirable endowments than others. The harms to patients with undersubscribed GPs are eliminated—they are equally well of as under the status quo. At the same time, patients with oversubscribed GPs retain the benefits of being able to trade GPs, and are still considerably better off than under the status quo.

### V.E Extensions

We find considerable scope for improving Norway's GP allocation mechanism through simple changes to the assignment algorithm and priority rules. However, our proposals hold many aspects of the mechanism fixed. In this section we consider two possible directions that would involve more dramatic changes: (i) eliminating waitlists, and (ii) allowing patients to join multiple GP waitlists. In both cases, our ability to predict equilibrium outcomes is limited to some degree, so we view these results as suggestive only.

Eliminating Waitlists. Many primary care systems otherwise similar to the one in Norway—including (to our knowledge) all HMOs in the U.S.—do not allow patients to join a waitlist for a GP who is currently not taking patients. A natural question is therefore whether introducing waitlists, as Norway did in 2016, in fact improves patient welfare. The answer is not obvious. Eliminating waitlists may mean that at any given time, more GPs are available immediately, but also that many GPs are not available to choose at all.

To attempt to evaluate this trade-off, we run a benchmark simulation, **No Waitlists**, in which an attentive patient may only choose among the GPs with open slots at the moment they consider switching. GPs are thus effectively rationed by "luck" due to stochastic availability, rather than through a first-come first-served priority system. We emphasize that outcomes arising from this simulation are not necessarily an equilibrium. In reality, patients would have an incentive to exert effort (e.g., frequently checking the website until a spot opens up) to obtain their desired GP. Nonetheless, this benchmark helps us assess whether eliminating

waiting times would likely come at a significant cost in terms of post-assignment match quality.

Column (3) of Appendix Table D.3 summarizes outcomes under this simulation. We find that mean patient welfare is slightly higher than under the status quo (0.19 minutes). Patients are reassigned to less-preferred GPs on average, but because waiting times are eliminated, patients spend less time mismatched with their current GP. This offsetting effect is especially valuable for patients with highly mismatched current GPs. It is therefore not so surprising that while mean welfare increases, median welfare decreases. The median patient is worse off relative to the status quo by 0.60 minutes. While patients with a highly-mismatched current GP benefit from the full elimination of waiting times, the majority of patients prefer an environment with more options and some waiting time. We interpret these results as suggesting that the desirability of introducing waitlists depends on how the gains for highly mismatched patients are weighed against the losses for patients who would prefer to wait for a more desirable option.

Joining Multiple Waitlists. An important restriction in all of our proposed mechanisms is that patients may only sit on one GP's waitlist at a time. This restriction fundamentally limits the mechanism's ability to find gains from trade because patients may only express that one GP is preferred to their current assignment. Allowing patients to submit longer or even unrestricted rank order lists could dramatically reduce waiting times if patients would rank many GPs. Moreover, if patients were roughly indifferent between many GPs, these reductions in waiting times could minimally impact ex-post match quality. Unfortunately, assessing the equilibrium implications of allowing patients to rank multiple GPs is challenging because such a change adds considerable computational complexity to a patient's choice problem.<sup>44</sup> We therefore instead consider a benchmark simulation, Truthful TTC, in which patients truthfully report their full preference list to the mechanism. This mechanism in effect allows patients to join an unlimited number of waitlists, but is implemented in such a way that we assume patients do so truthfully (i.e., patients join the waitlists for all GPs preferred to their current GP). The mechanism is formally described in Appendix D.4, and the results are

<sup>&</sup>lt;sup>44</sup>In static implementations of DA or TTC with unrestricted preference lists, patients can do no better than truthfully reporting their ordinal preferences. In a dynamic implementation of these algorithms, "strategy-proofness" would no longer hold. It may be optimal for a patient to truncate their true preference list to ensure that they receive a more desirable GP, even if they must wait longer. Calculating a patient's optimal truncation point requires calculating their continuation value from every possible truncated list. Even mechanisms which allow patients to rank a small number of GPs becomes complex in a market with many alternatives—if joining two waitlists were allowed, there are  $\binom{J}{2}$  possible rank-order lists. Further, these alternative designs would require modeling patients' beliefs about the joint distribution of waiting times across multiple waitlists, as well as modeling their strategic behavior under much more complex choice problems than those considered so far.

reported in column (4) of Appendix Table D.3.

Truthful TTC effectively eliminates waiting times—almost all patients can be reassigned to some preferred GP at the end of the same month in which they are attentive. This result is driven by the fact that most patients prefer many GPs to their current one (often including at least one undersubscribed GP), as well as the large degree of horizontal preference heterogeneity that exists. The reduction in waiting times does come at the cost of a less preferred assignment. The average preference rank of a patient's reassigned GP is 2.72 under Truthful TTC, compared to 1.79 under Waitlists and 1.63 under TTC. It is nonetheless striking that even when patients cannot choose to wait longer for a more highly preferred GP, most are still reassigned to one of their top few choices.

Although Truthful TTC is a very different proposal from No Waitlists, it has qualitatively similar impacts—it nearly eliminates waiting times, but leads to lower post-assignment match quality. Quantitatively, however, the loss in match quality under Truthful TTC is smaller than under No Waitlists (and the resulting welfare gains greater) because Truthful TTC also finds gains from trade among attentive patients, as opposed to only allowing assignments to vacancies. In fact, mean patient welfare is higher under Truthful TTC than under any of our proposed mechanisms. In terms of realized flow payoffs, patients are on average 1.04 minutes better off relative to Waitlists (compared to 0.75 minutes under TTC). However, as under No Waitlists, these gains are concentrated among a minority of patients; the median patient is no better off. In contrast, our primary proposals of TTC and TTCP modestly reduce waiting times, while still improving post-reassignment match quality, yielding more widely distributed gains.

## VI Conclusion

This paper studies the problem of dynamically reassigning a set of agents to a set of objects when agents' preferences over objects may change over time. Our application is Norway's primary healthcare system, in which individuals are matched with a GP throughout their whole life, and may over time wish to switch their assigned GP. We provide direct evidence of unrealized gains from trade under Norway's current reassignment mechanism, and suggest alternatives for improvement. To predict outcomes under alternative mechanisms, we estimate a structural model of patient demand for GPs and apply the estimates within a dynamic equilibrium model of a GP reassignment system. Our results suggest that applying

straightforward ideas from the market design literature—particularly the TTC algorithm—can reduce waiting times and improve patients' ability to obtain a well-matched GP. However, our results also highlight the fact that tools designed for static environments may have unintended consequences in a dynamic setting. In particular, introducing TTC within a dynamic reassignment system can leave some agents worse off relative to operating strictly first-come first-served waitlists. Patients who are matched with the least demanded GPs are especially disadvantaged. We then show that modifications to the priority system can eliminate harms to these patients while preserving about 60 percent of the gains from TTC.

The existence of formal waitlists in our empirical setting makes unrealized gains from trade directly visible to the researcher, but similar gains could very well be present in other settings where there is currently no formal way to register a desire to be reassigned. Canonical market design applications such as public housing, specialized labor markets, public school seats, and hunting permits share many of the features of our present study, and often lack centralized reassignment mechanisms. Reassignment mechanisms that do exist—for example, public housing transfer systems in the U.S., and public school reassignment systems in NYC and Chile—often use waitlists that are similar to Norway's.

Even so, our analysis leaves several design questions unexplored. Within the class of mechanisms we have considered, one could optimize on several dimensions we simply hold fixed—for example, the frequency with which the matching algorithm is run, the information made available to patients, or as discussed, the ability to join multiple waitlists. More broadly, this study raises the question of how scarce resources should be rationed in dynamic assignment settings where prices do not clear the market. Many, if not most, settings of this type do not use formal waiting lists, and instead require agents to "check back later" for availability, effectively rationing desirable objects through agent effort and luck rather than by waiting times. Finally, there is a question of whether to impose formal capacity constraints (as in Norway), or to allow the market to clear through endogenous quality degradation from overcrowding (as in England). With some extension, our framework could be useful for studying these questions.

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# Appendix A Data Details

#### A.1 Data Sources

The data for this study are derived from Fastlegedatabasen, maintained by the Norwegian Directorate of Health, as well as the administrative registries at Statistics Norway (SSB). Individuals in the data (both patients and GPs) are each assigned a unique identifier which can be merged across datasets. Patients' municipalities of residence are identified at the monthly level using information from Fastlegedatabasen. Monthly municipality of residence is carefully tracked in this data because municipalities make monthly transfer payments to one another when a patient residing in one municipality enrolls with a GP located in another.

The raw GP enrollment and waitlist data are provided at the enrollment spell and waitlist spell level, respectively. Enrollment spells start and end only on the first and last days of a month (and so are in increments of full months). Waitlist spells can begin and end in continuous time. The time at which an individual joins a waitlist governs their priority in the waitlist. We convert the spells data to an individual-month panel. If an individual is on multiple waitlists in the course of a month, we take the most recent waitlist they were on. For our primary analyses, we make only three restrictions: (i) dropping individual-months that occur after the individual's registered date of death, (ii) dropping individuals under age 16, and (iii) dropping individual-months in which no current GP was registered. Appendix Table A.1 shows the number of individual-months dropped by these restrictions. Children under age 16 represent 17 percent of the data and population.

Table A.1. Sample Construction Statistics

	6	2017		2018	2019	
Criteria	Number	Pct. of initial	Number	Pct. of initial	Number	Pct. of initial
Initial patient-months	63,437,631		63,813,290		64,212,740	
Registered after death	1,918	< 0.01	48	< 0.01	27	< 0.01
Age < 16	11,475,019	0.18	10,694,796	0.17	9,918,551	0.15
No current GP	1,801	< 0.01	2,066	< 0.01	2,810	< 0.01
Final total	51,958,893		53,116,380		54,291,352	

*Notes*: This table shows the number of patient-months each year dropped due to each sample selection criterion (in the order in which drops were made). The primary restriction on the data is to remove children under the age of 16.

## A.2 Construction of Demand Estimation Sample

We estimate our model using the set of (adult) patient-months where the patient is resident in the Trondelag region and the month is between December 2018 and November 2019. We make further restrictions relating to the definition and construction of patients' GP choice sets. Our baseline choice set definition is a 60 minute drive time radius around each patient's municipality of residence. Any individuals that were enrolled with or joined a waitlist for a GP further than 60 minutes driving time are dropped from the analysis. In addition, we drop patient-months in which the current or requested GP exited during the subsequent month. Finally, for patient-months in which no GP switch was requested, we drop observations where the patient was currently standing on a waitlist. These months reflect the outcome of a prior decision to join a waitlist, which we already capture in the set of patient-months where was a switch was requested.

Appendix Table A.2 describes the observations dropped at each step. We are left with 4,238,740 patient-months in which a switch was not requested, and 19,335 months in which a switch was requested. These observations together are informative about when patients are attentive and consider switching GPs. Conditional on making a switch request, the switchermonth observations are informative about which GP characteristics patients value.

Table A.2. Demand Estimation Sample Construction

	Non	Non-switches		witches
Criteria	Number	Pct. of initial	Number	Pct. of initial
Initial patient-months in Trondelag region	4,617,483		29,771	
Current GP further than 60 minutes	151,315	0.03	6,958	0.23
Requested a GP further than 60 minutes			2,976	0.10
Current GP exiting next month	158,457	0.03	404	0.01
Requested an exiting GP			98	< 0.01
Currently on a waitlist	68,971	0.01		
Final total	4,238,740		19,335	

Notes: This table describes the sample selection criteria used in constructing the demand estimation sample. The unit of observation is a patient-month, and location of residence is measured at the monthly level. "Switches" are patient months in which the patient either joined a waitlist or else switched to a GP with open slots. "Non-switches" are patient months where a patient took no action. Both switches and non-switches are used in demand estimation.

Given the large size of the data, we proceed with estimation using all switcher patientmonths and a random sample of 15,000 non-switcher patient-months. In estimation, we then re-weight the sampled non-switcher observations such that they represent the full set of observations. Given that patients with recent moves are disproportionately likely to be excluded from demand estimation because they hold a GP further than 60 minutes, we also adjust the sampling weights to match the original observed proportion of movers versus non-movers in both the non-switcher and switcher samples. Finally, once the random sample of non-switchers is drawn, we enforce a final restriction that all GPs remaining the analysis are chosen a sufficient number of times for a GP fixed effect to be estimated. We require each GP to be present in at least 400 individuals' choice sets. GPs that do not meet this requirement are dropped from all choices sets (and all patients that choose such a GP are also dropped). Our final estimation sample consists of 14,809 non-switcher months (re-weighted to represent 4,617,483) and 19,335 switcher months (re-weighted to represent 29,771).

# Appendix B Additional Analysis

### **B.1** Mechanical Simulations: Implementation Details

Implementation of TTC. Only patients on waitlists participate in the TTC algorithm, as any patient not standing on a waitlist retains their slot on their current GP's panel. TTC is thus run to find a matching between (a) the set of patients standing on waitlists, and (b) the set of GP panel slots currently held by those patients. Preferences are all strict and are determined as follows:

- (a) Patients standing on a waitlist first prefer their waitlist GP, then their current GP.
- (b) GPs first prefer all their incumbent patients who are participating in TTC. Since these patients must be waiting on a waitlist, they have a global priority order determined by the moment in time at which they joined that waitlist. GPs prefer their incumbent patients in order of this global priority. GPs then prefer all the patients on their waitlist in the order in which they joined (which again corresponds to this global priority).

We iteratively look for cycles within chains that begin with a patient, starting with the patient who is highest on the global priority list and going down the list from there.

Mechanical Simulation of TTC on Historical Data. We implement the TTC algorithm monthly on the historical waitlists data between November 2016 and December 2019. The purpose of this exercise is to generate a simple (but naive) estimate of how TTC would

have changed the waiting lists had it been in place during this period. In that spirit, we hold all of the following objects fixed as they are observed in the data: patient entry (births or immigration), patient exit (deaths or emigration), administrative auto reassignments of patients, GP entry, GP exit, GP panel caps, and, critically, patient actions. A patient's action each month can be (a) doing nothing and remaining with their current GP, (b) switching to an open GP, or (c) joining a waitlist for a full GP. We then run the TTC algorithm on all patients standing on waitlists each month. Patients who can participate in a cycle are reassigned to their desired GP's panel and removed from waitlists.

### **B.2** Preferences for GP Characteristics

This section investigates patient preferences for GP characteristics using a conditional logit analysis of GP choice. Given the size of the data, we limit attention to the geographic subsample of patients described in Section IV.A and Appendix A.2. Further, for the purposes of this specific analysis, we limit to the set of patient-months in which the patient requested to switch their GP, either by switching to an open GP or else by joining a waitlist. Within this subsample, we estimate the following conditional logistic regression specification:

$$u_{ijt} = -d_{ijt} + w_{ijt}\alpha + \delta_j + X_{ijt}\beta + \sigma_\epsilon \epsilon_{ijt} ,$$

where  $d_{ijt}$  is driving time between patient *i*'s municipality of residence and GP *j*'s office,  $w_{ijt}$  is the number of patients on GP *j*'s waitlist at the beginning of the month *t* when patient *i* made their switch request,  $\delta_j$  is a set of GP fixed effects,  $X_{ijt}$  includes interactions between patient and GP age and gender, and  $\epsilon_{ijt}$  is a type-1 extreme value idiosyncratic shock. We normalize the coefficient on driving time to -1.

Appendix Table B.1 reports results from three specifications. Column (1) excludes GP fixed effects and interactions between patient and GP characteristics. It controls only for GP age and gender, such that all horizontal GP differentiation comes from travel time and idiosyncratic taste shocks. Younger and female GPs are chosen more often, as are GPs with shorter waitlists. Column (2) adds observable patient-GP match-specific heterogeneity based on age and gender. Compared to male patients, female patients have a strong preference for female GPs; they would be willing to travel more than 5 minutes longer to see one. There

<sup>&</sup>lt;sup>45</sup>Temporary residents are treated as a distinct category because their demographic information is not available. We explored other GP and patient characteristics, and found few that were statistically and economically significant in explaining patients' GP choices.

is also clear, though weaker, homophily on age: all patient groups prefer younger GPs, but compared to a patient over age 45, a younger patient would travel about a minute longer to see a GP who is also under 45.

Table B.1. Preferences for GP Characteristics: Conditional Logit

	(1)	)	(2)		(3)	
Variable	$\beta$	SE	$\beta$	SE	$\beta$	SE
Travel time (minutes) <sup>†</sup>	-1.000		-1.000		-1.000	
Waitlist length	-0.026	0.002	-0.026	0.002	-0.090	0.006
Female GP	1.335	0.094				
$\times$ Temporary resident			2.490	0.247		
$\times$ Perm. res. female, age 16–45			3.723	0.173	1.209	0.274
$\times$ Perm. res. female, age 45+			2.838	0.189	0.131	0.286
$\times$ Perm. res. male, age 16–45			-1.910	0.221	-4.122	0.315
$\times$ Perm. res. male, age 45+			-2.461	0.258	-4.747	0.344
GP age 45+	-1.901	0.095				
× Temporary resident			-1.573	0.247		
$\times$ Perm. res. female, age 16–45			-2.353	0.168	-0.694	0.280
$\times$ Perm. res. female, age 45+			-1.544	0.183	0.060	0.290
$\times$ Perm. res. male, age 16–45			-2.118	0.217	-0.394	0.310
$\times$ Perm. res. male, age 45+			-1.343	0.243	0.303	0.329
Coeff. on epsilon shock	6.296	0.105	6.284	0.105	5.905	0.110
GP FE	N		N		Y	
Dep. variable mean	0.00	)5	0.00	5	0.00	5
# Observations	3,492,	876	3,492,	876	3,492,	876

Notes: This table reports coefficient estimates from conditional logistic regressions predicting the GP choices of patients who requested to switch GP between December 2018 and November 2019. The unit of observation is a (patient-month, GP) pair. The sample includes patient-months and GPs in Trondelag who meet the inclusion criteria for our structural estimation sample, with the additional restriction that each included GP is in at least 500 patient choice sets. The average patient-month has 192 GPs within choice set. Since this analysis conditions on requesting to switch, we exclude each patient's current GP from choice set. The outcome variable is an indicator for whether the patient requested to switch to a specific GP. GP FE indicates whether the specification includes a fixed effect for each GP, with one GP's fixed effect normalized to zero. In column (3), temporary residents serve as the omitted category for interactions between GP and patient characteristics. †By normalization

Column (3) adds GP fixed effects, absorbing any persistent GP-specific differences in desirability. The coefficients related to match specific heterogeneity—age and gender interactions and the standard deviation of the idiosyncratic shock—are very similar to column (2).<sup>46</sup> However, adding GP fixed effects more than triples the magnitude of the estimated coefficient on

<sup>&</sup>lt;sup>46</sup>The levels of the coefficients are different than in column (2) because column (3) normalizes the preferences of temporary residents for GP age and gender to zero, but the *difference* between any two coefficients is nearly unchanged.

waitlist length. This is consistent with more desirable GPs having longer waitlists. Column (3) isolates responsiveness to variation in the length of the same GP's waitlist (relative to other waitlists) over time. This type of variation occurs naturally in queues due to statistical fluctuations in the number and types of agents and objects arriving over time (Waldinger, 2021; Leshno, 2022). The sensitivity of patients' choices to waiting time (information) will be a key determinant of the equilibrium implications of changing the design of the waitlist mechanism.

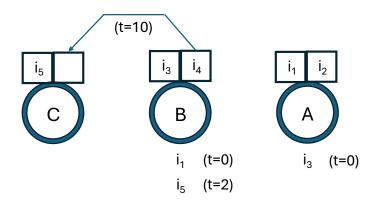
### B.3 TTC is Not Pareto Improving: Styled Examples

This section constructs simple examples in which TTC is and is not Pareto improving over Norway's status quo mechanism (Waitlists). We also compare to the patient-optimal stable match produced by DA, which is always Pareto improving over Norway's status quo mechanism. As in our mechanical simulations, each example holds initial assignments and patient switch requests fixed across assignment algorithms, and maintains FCFS priority among waiting patients. Section V.B formally describes each algorithm.

**Example 1.** We begin with an example in which TTC generates a Pareto improvement. Appendix Figure B.1 illustrates an economy with the following primitives:

- There are five patients  $(i_1, i_2, i_3, i_4, i_5)$  and three GPs (A, B, and C), each with a panel cap of two.
- At t = 0,  $i_1$  and  $i_2$  are assigned to A;  $i_3$  and  $i_4$  are assigned to B; and  $i_5$  is assigned to C. As a result, A and B have full panels, while C has an open slot.
- At t = 0,  $i_1$  requests to switch from A to B, while  $i_3$  requests to switch from B to A. Since there are no other waiting patients, each patient is placed at the front of their requested GP's waitlist.
- At t = 2, patient  $i_5$  requests to switch from C to B, and is placed behind patient  $i_1$  on B's waitlist.
- At t = 10, patient  $i_4$  requests to switch from B to C, which can be immediately executed because there is an open slot.
- At t = 20, patient  $i_2$  dies, vacating a slot on A's panel.

Figure B.1. Example 1: TTC Generates a Pareto Improvement



We now consider when each patient is reassigned under each assignment algorithm:

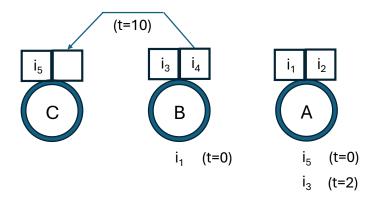
Waitlists: Under Norway's status quo mechanism, patients  $i_1$  and  $i_3$  cannot trade immediately, even though each is waiting for the other's GP. Instead, they must wait for a vacancy on either A's or B's panel. A vacancy arises at t = 10, when  $i_4$  requests to switch from B to C. Since C has an open slot, the following steps occur:  $i_4$  is assigned to C, creating a vacancy on B's panel;  $i_1$  is assigned to B from the front of the waitlist, creating a vacancy on A's panel;  $i_3$  is assigned to A from the front of the waitlist, creating another vacancy on B's panel; and  $i_5$  is assigned to B, creating a vacancy on C's panel. At this point, no patients remain on a waitlist. Thus, all patients who have requested to switch GP are reassigned at t = 10.

DA: We next consider the allocation produced by running patient-proposing DA each month, after filling any vacant slots from waitlists. At t=0,  $i_1$  and  $i_3$  are allowed to "trade" GPs since each is at the top of their respective waitlist. During the DA algorithm,  $i_1$  first proposes to B, and  $i_3$  first proposes to A; since neither patient is rejected, the algorithm terminates with each patient reassigned to their requested GP. Between t=0 and t=10, only patient  $i_5$  is waiting to switch GP, so DA produces no additional reassignments.  $i_5$  must still wait until t=10, when  $i_4$  open switches from B to C, to be reassigned to B. Thus, compared to Waitlists, DA allows patients  $i_1$  and  $i_3$  to be reassigned at t=0 instead of t=10, while  $i_5$  is still reassigned at t=10. This is a Pareto improvement because  $i_1$  and  $i_3$  wait for strictly less time, whereas  $i_5$  waits for the same amount of time.

TTC: In this example, the TTC algorithm produces the same allocations as DA. At t = 0, pairs  $(i_1, A)$  and  $(i_3, B)$  immediately form a cycle, so the two patients are reassigned. TTC produces no additional reassignments, and patient  $i_5$  is reassigned to B at t = 10, after patient  $i_4$  switches to C. Like DA, TTC generates a Pareto improvement relative to Waitlists.

**Example 2.** Figure B.2 illustrates an example that is identical to Example 1 except that (i) patient  $i_5$  requests GP A instead of B, and (ii) patients  $i_5$  and  $i_3$  request A in reverse order:  $i_5$  requests to switch from C to A at t = 0, while  $i_3$  requests to switch from B to A at t = 2. We again consider when each patient is reassigned under each algorithm.

Figure B.2. Example 2: TTC is not Pareto Improving



Waitlists: As in the previous example, no reassignments occur until t = 10. At t = 10, patient  $i_4$  open switches to C's panel, leaving a vacant slot on B's panel; patient  $i_1$  is reassigned to the vacant slot on B's panel, leaving a vacant slot on A's panel; and patient  $i_5$  is reassigned to the vacant slot on A's panel, leaving a vacant slot on C's panel. No further reassignments occur this period, and patient  $i_3$  remains on the waitlist for A. At t = 20, patient  $i_2$  dies, vacating a slot on A's panel which is reallocated to patient  $i_3$ . No further patients are waiting to switch GP. Thus, all waiting patients are reassigned at t = 10 except  $i_3$ , who is reassigned at t = 20.

DA: In this example, patients  $i_1$  and  $i_3$  could execute a mutually beneficial trade beginning in t = 2, when  $i_3$  joins GP A's waitlist. However, the DA algorithm will not execute this trade while patient  $i_5$  remains on A's waitlist because it would violate waiting time priority to reassign  $i_3$  before  $i_5$ . The specific steps would be as follows:

- In each period t = 2, 3, ..., 9, the DA algorithm would reassign zero patients, despite the potential gains from allowing  $i_1$  and  $i_3$  to trade. The sequence of proposals would be as follows.  $i_1$  first proposes to B and  $i_5$  and  $i_3$  propose to A; A provisionally holds  $i_5$ 's proposal and rejects  $i_3$ , who is lower on the waitlist. In the next round,  $i_3$  proposes to B (their current GP), who then rejects  $i_1$ . In the next round,  $i_1$  proposes to A, who then rejects  $i_5$ , who then proposes to C. At this point, all waiting patients propose to their current GPs, and since no patient is rejected, the algorithm terminates.
- At t = 10, DA reassigns the same patients that are reassigned under Waitlists (all except

- $i_3$ ). To see this, note that this is the patient-optimal *stable* match; reassigning  $i_3$  would require not reassigning  $i_5$ , which would violate waiting time priority.
- At t = 20, patient  $i_3$  is reassigned to A after patient  $i_2$  dies.

Thus, in this example, DA produces exactly the same outcomes as Waitlists because it cannot violate waiting time priority.

TTC: In this example, TTC produces a different allocation than Waitlists and DA, and in the process, harms patient  $i_5$  (while benefiting patients  $i_1$  and  $i_3$ ). At t=2, when  $i_3$  requests to switch from B to A,  $i_1$  and  $i_3$  form a cycle and trade GPs when the TTC algorithm is run. Patient  $i_5$  remains on the waitlist for GP A. At t=10, patient  $i_4$  open switches to panel C, vacating a slot on B's panel. This slot remains vacant since there are no patients waiting for B, and  $i_5$  remains on the waitlist for GP A. At t=20, patient  $i_5$  is reassigned to the slot vacated by  $i_2$ , who dies.

Compared to Waitlists and DA, patients  $i_1$  and  $i_3$  are reassigned 8 and 18 periods earlier, respectively, since they trade GPs at t=2 instead of being reassigned at (respectively) t=10 and t=20. However, patient  $i_5$ , whose GP is not oversubscribed, waits 10 periods longer, being reassigned at t=20 instead of t=10. This example illustrates how TTC not only moves reassignments forward in time, but also reallocates slots towards patients that can facilitate trades. Specifically, TTC allows patient  $i_1$ 's slot on A's panel to be reallocated sooner, reducing the total amount of time waited in the economy. However, it also reallocates  $i_1$ 's slot from patient  $i_5$ , who cannot form a cycle, to  $i_1$ , who can.

## **B.4** Predictors of Switching GPs

A number of patient characteristics appear predictive of a desire to switch GPs. For example, Table 1 shows that 34 percent of patients who had switched to an open GP and never used a waitlist over the period 2017–2019 had moved at some point during that period, compared only 6 percent of patients who had neither switched GP nor used a waitlist. To investigate the relative importance of various factors that may motivate GP switching, we regress an indicator for a GP switch request on patient characteristics. A GP switch request includes either an immediate switch to an open GP or a waitlist join. Our focal patient characteristics include time-invariant patient demographics and the timing of a switch relative to a move.

Appendix Table B.2 reports these results. The outcome variable (the switching indicator) is scaled by 100 for readability, so coefficients should be interpreted as percentage points. The

overall probability of observing a switch request is 0.718 percent. Specification (1) includes only a set of five mutually exclusive and exhaustive patient demographic types. We find that temporary residents are substantially more likely to request to switch GPs than permanent residents, with a baseline probability of 1.501 percent. Among permanent residents, younger patients (particularly females) are more likely to switch.

Table B.2. Predictors of Switching GPs

	(1)		(2)	
Variable	β	SE	β	SE
Patient demographic category				
Temporary resident	1.501	0.005	1.302	0.005
Perm. res. female, age 16–45	1.171	0.002	0.952	0.002
Perm. res. female, age 45+	0.501	0.001	0.459	0.001
Perm. res. male, age 16–45	0.782	0.001	0.568	0.001
Perm. res. male, age 45+	0.375	0.001	0.326	0.001
Timing relative to move				
Move in $[t-6, t-1]$ ; <30 min.			1.428	0.013
Move in $[t-6, t-1]$ ; $\ge 30$ min.			3.243	0.013
Move in $[t, t+1]$ ; $<30$ min.			3.471	0.031
Move in $[t, t+1]$ ; $\geq 30$ min.			11.451	0.037
Dep. variable mean	0.71	.8	0.71	8
$R^2$	0.009		0.02	1
# Observations	154,793	3,455	154,793	3,455

Notes: This table investigates observable predictors of requesting to switch GPs. The unit of observation is the patient-month. The sample includes all adult patients in Norway over the period January 2017 to November 2019. Regressions are linear probability models where the outcome variable is an indicator for a GP switch request (either a waitlist join or a switch to a GP panel with open slots). All covariates are indicator variables. For readability, the outcome variable is scaled by 100; coefficients should therefore be interpreted as percentage points.

Specification (2) introduces information on the timing of a given patient-month relative to a patient move. Conditional on a move being observed in the past 6 months, the current month, or the next month, we create four categories of moves based on an intersection of timing and distance of move. We find that switches are substantially more likely to occur in the month concurrent with or directly preceding the month of a move, and also that switches are far more likely to be associated with longer moves relative to shorter moves. For example, someone moving over 30 minutes away either this month or next month (i.e., in month [t, t+1]) has an extra 11.451 percent chance of requesting to switch GPs. Variation induced by moves therefore appears, unsurprisingly, to be an important determinant of when patients

### B.5 Responsiveness to Aggregate Waitlist Length

An important question in our counterfactuals is whether more patients would request to switch GPs if expected waiting times fell systematically. Such a response would be predicted by a model where patients pay a "switching cost" at the time they request to switch GPs. In contrast, our proposed model of exogenous inattention rules out this type of response. As there is no direct switching cost, an attentive patient will always request to switch GP if any GP is preferable to their current one.

Testing for such a response is challenging because it requires aggregate variation in waitlist lengths, holding other demand and supply conditions fixed. One observation we can make is that the rates of switch requests have remained steady since waitlists were introduced in November 2016, and the number of waiting patients has grown almost linearly since then. If patients were more likely to make switch requests when waiting times were shorter, we would have expected a spike and then decline in switch requests after the introduction of waitlist. The time series evidence therefore weighs against a fully attentive model. However, it is also possible that patients gradually became aware of the new waitlist system, offsetting a deterring effect of increasing waiting times. We therefore also look for shorter-term variation in aggregate waitlist lengths.

Another source of variation that occurred during our sample period—but before the period used for structural estimation—systematically reduced both perceived and actual waiting times. Until October 2017, Norway maintained a "buffer" of 20 slots on each GP's panel, and only assigned waiting patients after 20 slots were available.<sup>47</sup> The buffer was intended to prevent other additions to a GP's panel, such as births and administrative reassignments, from violating the panel cap. However, recognizing that this buffer kept patients waiting for GPs with open slots, the buffer was reduced from 20 to 10 slots in October 2017. GPs with 10–19 open slots had their panels filled with patients from the waitlist at the end of the month, resulting in a one-time drop in aggregate waitlist lengths. We use this variation to test whether aggregate switching rates increased immediately after this policy change, both overall and differentially by the amount different geographic regions were impacted.

Figure B.3 plots the monthly share of patients requesting to switch GP in a two-year window

 $<sup>^{47}</sup>$ The algorithm would fill all of the open slots once the buffer was exceeded, so a given GP did not always have 20 extra slots.

around the month of the buffer change. Monthly switching rates range between 0.5 percent and 1 percent, but there is no visible increase in the aggregate number of switch requests beginning in October 2017. While there is not a clear aggregate response in switching requests, there was substantial variation across municipalities in the extent to which the change in the waitlist buffer affected waitlist lengths. In particular, smaller municipalities were much more affected. We can therefore explore geographic heterogeneity in the impact of the buffer change.

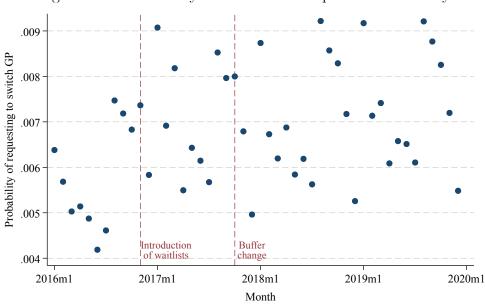


Figure B.3. Probability of GP Switch Request: Event Study

*Notes*: The figure shows the average rate of GP switch requests in Norway over time, where a switch request includes both joining a waitlist and switching to an open GP. Waiters were introduced in November 2016. The waitlist buffer was reduced from 20 to 10 in October 2017.

The GPs directly impacted by the buffer change were those with 10–19 slots available prior to the change. For these GPs, all available slots were filled once the buffer was reduced to 10, but would not have been had the buffer remained at 20. We measure exposure to the buffer change in two ways. First, we calculate the fraction of GPs in each municipality who are near the buffer ("Near-Buffer"), meaning they had 10–19 open slots on their panel as of September 2017. Second, since waitlist lengths varied among Near-Buffer GPs, we multiply each municipality's Near-Buffer share by the average change in the length of the waitlist among Near-Buffer GPs. This measure isolates the average change in the length of all GP waitlists induced by the buffer change, which is more than 1.5 patients in the median municipality. We interact both measures with indicators for 1–3 and 4–12 months after the buffer change. Table B.3 reports these results. We find no differential impact of these exposure measures on switching rates, regardless of whether or not we control for a linear time trend in switching

rates.

Table B.3. Switch Requests by Exposure to Buffer Change

	Near Buffer			Waitlist Change				
	(1)	)	(2)	)	(1)		(4)	
Variable	β	SE	β	SE	β	SE	β	SE
OctDec $2017 \times 1$ S.D. Exposure	0.120	0.153	0.121	0.153	0.000	0.117	-0.000	0.117
JanOct 2018 $\times$ 1 S.D. Exposure	0.153	0.135	0.154	0.135	-0.155	0.117	-0.155	0.117
Trend			-0.000	0.011			-0.000	0.011
Municipality FEs	Y		Y		Y		Y	
Month FEs	Y		N		Y		N	
Dep. variable mean	0.00	9	0.00	9	0.00	9	0.00	9
# Observations	10,4	24	10,45	24	10,4	24	10,4	24

Notes: The table reports estimates from linear regressions predicting the share of residents within a municipality-month who request to switch GP, weighted by population. The sample includes all municipality-months between October 2016 and October 2018. The outcome variable is the share of residents who requested during that month to switch to a new GP. In Columns (1) and (2), exposure is defined as the share of GPs "Near Buffer," i.e. with 10–19 open slots as of September 2017. In Columns (3) and (4), exposure is defined as "Waitlist Change," the change in waitlist length from September to October 2017 interacted with an indicator for GPs being near the buffer. Both measures are in standard-deviation units. All coefficients and standard errors are scaled by 1,000 for readability.

# Appendix C Estimation Details

This section provides details on the Gibbs' Sampler used to estimate the structural model parameters. We first describe the restrictions that the choice data place on the model primitives; then how we draw patient attention  $\lambda_{it}$  and flow payoffs  $v_{it}$ ; and finally, how we update the discount rate  $\rho$ . The updating steps for  $(\beta, \sigma_{\epsilon})$  are standard. Unless otherwise specified, we condition on the month t in what follows and omit it from the notation.

Restrictions on Primitives. Consider a patient i with current GP  $j_0$  who requests to switch in a given month. We learn two things from this patient. First, since they requested to switch GP, they were attentive:  $\lambda_i = 1$ . Second, their chosen GP  $j^*$  must have higher expected net present value than any other GP, given the patient's preferences and waiting time beliefs:

$$\underbrace{\mathbb{E}\left[e^{-\rho T_{ij^*}} \mid \mathbf{w}_i\right]}_{\omega_{j^*}(\rho)} (v_{ij^*} - v_{ij_0}) \ge \underbrace{\mathbb{E}\left[e^{-\rho T_{ij}} \mid \mathbf{w}_i\right]}_{\omega_{j}(\rho)} (v_{ij} - v_{ij_0}) \quad \forall j \in \mathcal{J}, \tag{6}$$

where we define  $\omega_j(\rho)$  to be the expected discount factor to simplify notation. This set of inequalities implies a lower bound on the flow payoff  $v_{ij^*}$  from the chosen GP, and an upper

bound on the flow payoff  $v_{ij}$  from each GP that was not chosen:

• Upper Bound: Rearranging Equation (6), for each  $j \in \mathcal{J} \setminus j^*$ ,

$$v_{ij} \leq \underbrace{\frac{\omega_{j^*}(\rho)}{\omega_j(\rho)} v_{ij^*} - \frac{\omega_{j^*}(\rho) - \omega_j(\rho)}{\omega_j(\rho)} v_{ij_0}}_{ub_{ij}(v_{ij^*}, v_{ij_0}; \rho)},$$

where the notation  $ub_{ij}(v_{ij^*}, v_{ij_0}; \rho)$  will be useful later.

• Lower Bound For chosen  $j^*$ ,

$$v_{ij^*} \ge \underbrace{\max_{j \in \mathcal{J} \setminus j^*} \frac{\omega_j(\rho)}{\omega_{j^*}(\rho)} v_{ij} + \underbrace{\frac{\omega_{j^*}(\rho) - \omega_j(\rho)}{\omega_{j^*}(\rho)} v_{ij_0}}_{lb_{ij^*}(\mathbf{v}_{i};\rho)}.$$

For patients who do not request to switch, it is not known whether they were paying attention. If the patient was not attentive  $(\lambda_i = 0)$ , then not switching contains no information about their preferences. If the patient was attentive  $(\lambda_i = 1)$ , then not switching implies that their current GP was preferable to all others:  $v_{ij_0} \ge \max_{j \ne j_0} v_{ij}$ .

Attention and Flow Payoffs. The Gibbs' sampler uses data augmentation to draw patients' attention and flow payoffs. The key challenge in drawing attention is calculating the likelihood that a non-switcher was attentive. By Bayes' Rule,

$$Pr(\lambda_{i} = 1 \mid \text{no switch}, X, j_{0}; \theta) = \frac{Pr(\text{no switch} \mid \lambda_{i} = 1, X, j_{0}; \theta) Pr(\lambda_{i} = 1)}{Pr(\text{no switch} \mid X, j_{0}; \theta)}$$

$$= \frac{Pr(\text{no switch} \mid \lambda_{i} = 1, X, j_{0}; \theta) Pr(\lambda_{i} = 1)}{Pr(\lambda_{i} = 0) + Pr(\text{no switch} \mid \lambda_{i} = 1, X, j_{0}; \theta) Pr(\lambda_{i} = 1)},$$
(7)

where  $\theta = (\rho, \beta, \sigma_{\epsilon}(\cdot), p^{\lambda}(\cdot))$  collects the model parameters. By definition,  $Pr(\lambda_i = 1) = p^{\lambda}(X_i)$  and  $Pr(\lambda_i = 0) = 1 - p^{\lambda}(X_i)$ , and we can express

$$Pr(\text{no switch } | \lambda_i = 1, X, j_0; \theta) = Pr(v_{ij_0} \ge \max_{j \ne j_0} v_{ij} | X; \theta)$$

$$= \int_{-\infty}^{\infty} \Phi\left[\Pi_{j \ne j_0} \left(\frac{v_{ij_0} - X_{ij}\beta}{\sigma_{\epsilon}}\right)\right] \phi\left(\frac{v_{ij_0} - X_{ij}\beta}{\sigma_{\epsilon}}\right) dv_{ij_0}, \quad (8)$$

where  $\Phi(\cdot)$  and  $\phi(\cdot)$  are the standard normal CDF and PDF, respectively. For each inattentive patient, the estimator evaluates this integral using Gauss-Hermite quadrature. Each patient's  $\lambda_i$  is an iid Bernoulli draw with probability defined in Equation 8 for non-switchers. The

attention probabilities  $p^{\lambda}(x)$  are then drawn from their posterior Beta distributions, given attention draws across all periods t:

$$p^{\lambda}(x) \mid \{\lambda_{it}\} \sim \text{Beta}\left(\alpha + \sum_{(i,t):X_{it}=x} \lambda_{it}, \varphi + \sum_{(i,t):X_{it}=x} (1 - \lambda_{it})\right),$$
 (9)

where the prior is  $Beta(\alpha, \varphi)$ . In practice, we resample the individual attention draws and parameters every 10 iterations of the Gibbs' sampler.

Drawing patients' flow payoffs for each GP is more straightforward. For attentive patients, we redraw the flow payoff from each non-chosen GP from a truncated normal distribution with upper bound  $ub_{ij}(v_{ij^*}, v_{ij_0}; \rho)$ , and the flow payoff  $v_{ij^*}$  for the chosen GP from a truncated normal distribution with lower bound  $lb_{ij^*}(\mathbf{v}_i; \rho)$ .

**Discount Rate.** The discount rate is updated via a Metropolis-Hastings step which requires calculating the likelihood of the data given the other parameters. The algorithm begins with a previous draw  $\rho_{b-1}$  and a proposal distribution  $F_{\rho}(. \mid \rho_{b-1}; \tau)$ , which is truncated normal.<sup>48</sup> Each iteration, the following steps occur:

- (i) Take a draw  $\tilde{\rho}_b \sim F_{\rho}(. \mid \rho_{b-1})$
- (ii) Calculate the ratio  $r(\tilde{\rho}_b, \rho_{b-1}) = \frac{L(\tilde{\rho}_b)}{L(\rho_{b-1})}$ , where  $L(\rho)$  is the likelihood of the data given  $\rho$  and the other current draws of the model parameters.

(iii) Set 
$$\rho_b = \begin{cases} \tilde{\rho}_b & w.p. & \min\{1, r(\tilde{\rho}_b, \rho_{b-1})\} \\ \rho_{b-1} & w.p. & 1 - \min\{1, r(\tilde{\rho}_b, \rho_{b-1})\} \end{cases}$$
.

The main difficulty in implementing this is calculating the likelihood

$$L(\rho) = \Pi_{i:\lambda_i=1} \ Pr\left(j^* = \arg\max_{k \neq j_0} \ \mathbb{E}\left[e^{-\rho T_{ik}}\right] \left(v_{ik} - v_{ij_0}\right) \mid \mathbf{X}_i, \mathbf{w}_i, \beta, \sigma_{\epsilon}, \rho\right)$$
(10)

for different values of the discount rate. This likelihood does not have a simple closed form, but it can be approximated with a high degree of accuracy using quadrature and exploiting the fact that the flow payoffs are conditionally independent given  $v_{ij_0}$ . Specifically, we can

<sup>&</sup>lt;sup>48</sup>We experimented with an adaptive variance parameter  $\tau$ , but settled on fixing  $\tau = 0.001$ .

rewrite each probability in equation 10 as

$$L_{i}(\rho) = \int_{-\infty}^{+\infty} \int_{v_{ij_{0}}}^{\infty} Pr(v_{ik} \leq ub_{ik}(v_{ij}, v_{ij_{0}}; \rho) \quad \forall k \neq j, j_{0} \mid \beta, \sigma_{\epsilon}) \ dF_{ij}(v_{ij}) \ dF_{ij_{0}}(v_{ij_{0}})$$

$$= \int_{-\infty}^{+\infty} \int_{v_{ij_{0}}}^{\infty} \prod_{k \neq j^{*}, j_{0}} \Phi\left(\frac{ub_{ik}(v_{ij^{*}}, v_{ij_{0}}; \rho) - X_{ik}\beta}{\sigma_{\epsilon}}\right) \ dF_{ij}(v_{ij}) \ dF_{ij_{0}}(v_{ij_{0}}), \tag{11}$$

where the last equality exploits conditional independence of  $v_{ik}$  given the flow payoffs from the patient's current and chosen GPs. To reduce the dimensionality of the integral, we condition on the value of  $v_{ij_0}$  when evaluating it, and evaluate the inner integral using Gauss-Laguerre quadrature.

# Appendix D Counterfactual Simulation Details

### D.1 Simulated Economy

As described in Section V.A, the simulated economy contains a finite set of patients I and GPs J. Patients have type  $x \in \mathcal{X}$ , where  $\mathcal{X} = \{\text{demographic type, location of residence}\}$ . GPs have type  $z \in \mathcal{Z}$ , where  $\mathcal{Z} = \{\text{demographic type, office coordinates, panel cap}\}$ .

GP characteristics are fixed over time. Patient characteristics evolve according to a stationary Markov process  $M: \mathcal{X} \to \mathcal{X}$ . Patients are assumed to indefinitely retain their gender ({Perm. res. female, Perm. res. male, Temp. res.}), so aging is the only relevant demographic transition. The transition process can therefore be thought of as drawing two independent shocks: a moving shock and an aging shock, where the probability of both shocks depends on a patient's current demographic type and location of residence. We calibrate transition probabilities to match observed transitions in Trondelag over 2017–2019. We then adjust the transition process to make it stationary.

Appendix Table D.1 reports details of the distribution of patient and GP types as well as the patient type transition process. Panel A describes patients. Seven percent of patients are temporary residents. Among permanent residents, half are female (with the remainder male), and 46 percent are age 16–45 (with the remainder 45 or older). Across all patients, the average probability of receiving an aging shock is 0.19 percent and the average probability of receiving a moving shock is 0.21 percent. The probability of aging is highest for temporary residents and lowest for females over age 45. The probability of moving is highest for female

under age 45 and lowest for females over age 45. Conditional on moving, patients are more likely to move to a nearby location than a distant location. Given the observed distribution of patient and GP locations, the average patient has 94 GPs within 15 minutes' driving time and 190 GPs within 60 minutes driving time, but there is substantial heterogeneity. In some rural areas, patients have only 5 GPs within 60 minutes, while in the central city of Trondheim, there are 189 GPs within only 15 minutes.

Table D.1. Fundamentals of Simulated Economy

			Percentile				
	Mean	Min	25th	50th	75th	Max	
Panel A: Patients ( $N = 371,536$ )							
Demographic Type							
Temporary resident	0.07						
Perm. res. female, age 16–45	0.21						
Perm. res. female, age 45+	0.26						
Perm. res. male, age 16–45	0.22						
Perm. res. male, age 45+	0.25						
Other Characteristics							
Prob. aging shock	0.002	0.001	0.002	0.002	0.002	0.007	
Prob. moving shock	0.002	< 0.001	0.001	0.002	0.002	0.012	
Num. GPs within 15 min.	95	0	15	34	189	189	
Num. GPs within 60 min.	190	5	73	262	262	279	
Travel time to avg. GP	94	47	47	60	118	523	
Panel B: GPs $(N = 425)$							
Demographic Type							
Female, age $\leq 45$	0.31						
Female, age>45	0.17						
Male, age≤45	0.25						
Male, age>45	0.27						
Other Characteristics							
Panel cap	930	80	794	936	1,098	1,695	
Travel time to avg. municipality	210	97	100	135	281	746	
Travel time to closest municipality	6	3	5	6	7	23	
GP fixed effect	-1.0	-10.5	-1.3	-1.1	-0.7	5.6	
Panel C: Locations $(N = 45)$							
Population	8,256	46	1,318	3,144	5,658	163,939	
Pct. temp. res.	0.06	0.02	0.05	0.06	0.07	0.10	
Pct. perm. res. female	0.47	0.41	0.46	0.46	0.47	0.54	
Pct. perm. res. ≤45	0.37	0.21	0.33	0.36	0.40	0.52	

*Notes*: The table describes the fundamentals of our simulated economy. These fundamentals are calibrated to match the Trondelag region as of December 2019. The 45 patient locations correspond to municipalities in the Trondelag region.

Panel B of Table D.1 describes the 425 GPs in the simulated economy. 48 percent of GPs are female, and 56 percent are under age 45. Among female GPs, however, 65 percent are under 45, reflecting growth of gender equity in this profession in recent decades. The average GP has a panel cap of 930 patients. The smallest GP has a cap of 80, while the largest has a cap of 1,695. For the purpose of our simulations, we do not use the panel caps observed in the data, but rather let them be determined based on the set of patients used in the simulation. For GPs that have waitlists as of December 2019, we set their panel cap equal to the observed number of patients that are enrolled with that GP and who reside in the Trondelag region. For GPs without waitlists, we set their panel cap equal to their observed enrollment among Trondelag patients times their observed ratio of enrollment to panel cap in the full data.

Finally, Panel C of Table D.1 describes the 45 possible locations where patients may live. The largest location is Trondheim municipality, with a population of 163,939 (nearly half the total population in the economy). The smallest location is Røyrvik municipality, with a population of only 46. The average location has 6 percent temporary residents, 47 percent female permanent residents, and 37 percent young permanent residents. Urban locations have a higher fraction of temporary residents as well as young permanent residents.

## D.2 Algorithm to Compute Equilibrium

For each mechanism, we compute a stationary equilibrium in which patients' beliefs about waiting time are consistent the waiting times implied by patients' optimal decisions. We initialize the economy to have no patients standing on waitlists (i.e., no patients in the reassignment mechanism). We draw a sequence of patient types (demographic type, location of residence, identity of mother if reborn) and patient attention shocks for 500 periods (months) for all 371,536 patients in our simulation. These draws are held fixed across counterfactual mechanisms.

We search for a fixed point between patients' belief parameters  $\mathbf{b} = (\eta, \kappa, \kappa_{OS}, \chi_0, \chi_1)$  and their sample analogs within the simulated economy. The algorithm works as follows. Iteration q begins with a vector of belief parameters  $\mathbf{b}^q$ . The following steps then occur:

(1) The simulation is run for 500 periods. Each period, the steps described in Section V.A occur, with all demographic transitions and attention shocks predetermined. Each period, attentive patients sequentially enter the reassignment mechanism and consider all GPs in the economy, observing their current waitlist lengths. Patients form beliefs about

waiting time according to  $\mathbf{b}^q$  and then decide which GP to choose. If they choose their current GP or an open GP, they are reassigned immediately and exit the mechanism. If they choose a GP with a waitlist, they wait there until they are successfully reassigned by the mechanism, they get another attention shock, or they die.

- (2) The simulation provides data on the distribution of realized waiting times given the optimal actions implied by beliefs  $\mathbf{b}^q$ . We use this information to construct the sample analog of belief parameters, relying only on the last 100 periods of the simulation to allow the economy to converge to a stationary distribution.
- (3) Beliefs are then updated as a convex combination of the initial and implied values:  $\mathbf{b}^{q+1} = \lambda^q \mathbf{b}^q + (1 \lambda^q) \mathbf{b}'$ . The factor  $\lambda^q$  determines how quickly beliefs are updated.

Implied beliefs. Table D.2 reports equilibrium belief parameters. Under the status quo Waitlists mechanism, 0.52 percent of panel slots become vacant each month. Under the mechanisms with TTC, such natural vacancies arise less frequently (0.10 percent per panel slot per month), since many incumbent patients who switch away no longer leave a vacant seat in their wake.

While TTC lowers the panel vacancy rate, it raises the waitlist departure rate, as waiters may now participate in a cycle. Under TTC, all patients perceive this rate as 4.68 percent per waiter ahead of them per month. Under TTCP, patients with undersubscribed GPs perceive it to be only 0.76 percent, since the only patients ahead of them on waitlists are other patients with undersubscribed GPs, who have no chance of participating in a cycle. Under TTC, a patient with an oversubscribed GP who is 10th on the waitlist for a GP with a panel cap of 1,000 believes they will participate in a cycle with probability  $0.132 = \exp(-4.9074 - 0.6273 \times \log(10/1000))$  each month. As their position-relative-to-panel-cap increases, this probability declines log-linearly. The same patient expects to participate in a cycle with monthly probability 0.031 in waitlist position 100.

Appendix Figure A.5 provides a depiction of how our beliefs model translated into expected waiting times and discount factors across mechanisms. A patient with an oversubscribed GP believes that the expected waiting time (in months) for a GP with panel size 1,000 with a waitlist length of 100 would be 18.0 under Waitlists, 16.8 under TTC, 18.0 under TTCP, and 18.0 under DA. For a patient with an undersubscribed GP, the corresponding beliefs would be 18.0 under Waitlists, 37.5 under TTC, 97.6 under TTCP, and 18.0 under DA. Note, however, that because patients with an undersubscribed GP get waitlist priority under TTCP, they

would rarely find themselves so far back on a waitlist. Appendix Figure A.6 reports the density of observed chosen waitlist lengths across mechanisms. Under TTCP, almost all the mass of chosen waitlist length is below a waitlist rank of 25. Finally, Appendix Figure A.7 provides a depiction of how our beliefs model interacts with panel capacities. Under the TTC mechanism, a patient with an oversubscribed GP believes that for a GP with a waitlist length of 50, expected waiting time would be 14 months if the GP had panel capacity of 750 and 11 months if capacity were 1,250. The average panel cap among GPs in our simulation is 930 (c.f. Appendix Table D.1).

Table D.2. Equilibrium Beliefs

	Waitlists	TTC	TTCP	DA
Panel vacancy rate $(\eta)$	0.0052	0.0010	0.0007	0.0052
Waitlist departure rate $(\kappa)$	0.0074	0.0468	0.0076	0.0074
Waitlist departure rate, curr. GP oversub. $(\kappa_{OS})$	_	_	0.0386	_
Cycle participation rate, curr. GP oversub. $(\chi_1)$		-4.9074	-4.7997	
Cycle participation rate, curr. GP oversub. $(\chi_2)$		-0.6273	-0.5816	

Notes: The table reports equilibrium belief parameters. In the TTCP mechanism, patients beliefs about the waitlist departure rate among waiters in front of them are  $\kappa$  for patients with an undersubscribed GP and  $\kappa + \kappa_{OS}$  for patients with an oversubscribed GP. In all other mechanisms, patients have common beliefs about  $\kappa$ . For patients with an oversubscribed GP, the perceived probability of participating in a cycle in waitlist position s for a desired GP with panel cap N is given by  $\chi = \exp(\chi_0 + \chi_1 \log(s/N))$ .

## D.3 Welfare Decomposition

A natural way to understand welfare under alternative mechanisms is to compare the NPV of an attentive patient's optimal choice of GP, which accounts for both the waitlist lengths they face when making a GP choice as well as their beliefs about how fast waitlists will move. Such a comparison is complicated, however, by the fact that at any given moment of attention, patients' current GP may change across mechanisms due to prior attention shocks. Since their degree of (dis)satisfaction with their current GP will directly affect how long they are willing to wait for a new GP, a patient's current GP is an important factor driving optimal choices. It is therefore useful to decompose NPV differences across mechanisms into (i) the component driven by a change in a patient's current GP, and (ii) the component driven by everything else, namely waitlist lengths, beliefs about how waitlist lengths map to wait times, and patients' optimal GP choice conditional on current GP.

To perform this decomposition, we introduce some additional notation. Throughout, we consider a single attentive patient in a single period whose preferences are held fixed across

mechanisms. Express an attentive patient's perceived NPV from choosing GP j while currently enrolled with GP  $j_0$  as

$$NPV(j; j_0, \mathbf{w}, \xi) = \mathbb{E}\left[\int_{\tau=0}^{T_j} e^{-\rho\tau} v_{j_0} d\tau + \int_{\tau=T_j}^{\infty} e^{-\rho\tau} v_{ij} d\tau \mid \mathbf{w}, \xi\right], \tag{12}$$

where **w** represents the vector of waitlist lengths for all GPs,  $\xi$  represents the patient's beliefs about the mapping from waitlist lengths to waiting time  $T_j$ , and  $v_j$  represents the per-period flow utility the patient derives from GP j. The NPV derived from a patient's optimal choice of GP is then given by

$$NPV^*(j_0, \mathbf{w}, \xi) = \max_{j \in \mathcal{J}} NPV(j; j_0, \mathbf{w}, \xi),$$
(13)

where  $\mathcal{J}$  is the set of all GPs. We can now isolate differences in the value derived from optimal behavior under each mechanism by differences in the arguments of  $NPV^*$ . As in Section V.D, we use the current Waitlists mechanism as our reference point. To that end, define the difference in the value derived from optimal behavior under focal mechanism M relative to the reference mechanism W as

$$\Delta NPV^{*,M-W} = NPV^*(j_0^M, \mathbf{w}^M, \xi^M) - NPV^*(j_0^W, \mathbf{w}^W, \xi^W), \tag{14}$$

where  $j_0^M$  is the patient's current GP under mechanism M,  $\mathbf{w}^M$  is the vector of prevailing waitlist lengths under mechanism M, and  $\xi^M$  is the patient's beliefs about the mapping from waitlist lengths to wait times under mechanism M. Given this notation, we can then express the decomposition as

$$\Delta NPV^{*,M-W} = NPV^{*}(j_{0}^{M}, \mathbf{w}^{M}, \xi^{M}) - NPV^{*}(j_{0}^{W}, \mathbf{w}^{M}, \xi^{M})$$
 (i)

$$+ NPV^*(j_0^W, \mathbf{w}^M, \xi^M) - NPV^*(j_0^W, \mathbf{w}^W, \xi^W), \tag{ii}$$

where as noted above, line (i) is the component of the welfare difference driven by a change in a patient's current GP, and line (ii) is the component driven by everything else, namely waitlist lengths, beliefs about how waitlist lengths map to wait times, and patients' optimal GP choice *conditional on current GP*. Because it more accurately represents the contemporaneous difference in the value of switching opportunities under different mechanisms, component (ii) is reported in the main text (Tables 5 and 6).

#### D.4 Benchmark Simulations

**No Caps.** Each GP's panel cap is infinite, so an attentive patient may switch to any GP immediately. This simulation provides an upper bound on the welfare that can be achieved by any mechanism with capacity constraints.

No Waitlists. An attentive patient may switch to any GP panel with open slots, but may not request a GP whose panel is currently full. The GP choice action is therefore a discrete choice among all open GPs plus the patient's current GP. We run the simulation under the assumption that patients are not strategic about when to request a GP (attention shocks are exogenously timed). Because there are no waitlists, no patients remain in the mechanism between periods.

**Truthful TTC.** This mechanism is identical to TTC with the exception that patients can submit ROLs of arbitrary length. We run the simulation under the assumption that when they arrive to the mechanism, attentive patients truthfully report their full ordinal preferences over GPs, truncated at their current GP.

Table D.3. Results from Benchmark Simulations

		Waitlists	TTC	No Waitlists	Truthful TTC	No Caps
GP waitlists						
Pct. of population	on a waitlist	9.36	8.88	_	0.03	_
Pct. of GPs with a	a waitlist	82.2	78.3	_	32.3	-
Mean E(waittime)	curr. GP undersub.	16.7	22.8			_
	curr. GP oversub.	16.7	10.7			_
Attentive patient ch	oices					
Mean E(waittime)	at chosen GP	16.8	14.1			_
Pct. waitlist joins		85.2	84.6	_	93.6	_
	curr. GP undersub.	79.0	74.8	_	92.3	_
	curr. GP oversub.	86.2	86.3	_	94.1	_
True pref. rank of	chosen GP	1.79	1.63	2.90	2.72	1.00
	curr. GP undersub.	1.94	2.29	2.87	2.67	1.00
	curr. GP oversub.	1.76	1.52	2.94	2.74	1.00
Realized assignment	is s					
Travel time to cur	rent GP, mean (med.)	17.3(6.5)	16.9(6.4)	16.8(6.5)	16.8(6.5)	16.8(6.4)
Pct. with same ge	nder GP   young female	59.3	60.3	58.5	58.6	68.7
	young male	61.8	61.2	60.9	61.2	52.6
Welfare						
Flow payoff from o	current GP, mean (med.)	_†	0.75 (0.69)	0.19 (-0.60)	$1.04 \ (0.01)$	5.34(4.53)

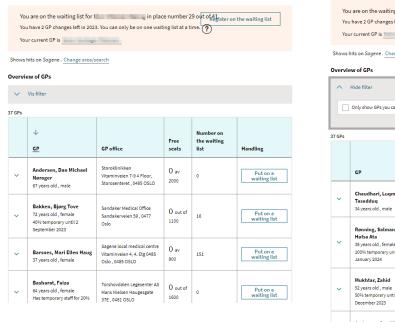
Notes: The table reports results under the benchmark simulations of No Waitlists and Truthful TTC (described in Section V.E). Results for Waitlists, TTC, and No Caps are reproduced from Table 5. Statistics are generated in months 392–451 of the simulation, out of 500 total months. They are first computed within month and then averaged across simulation months. E(waittime) is the expected waiting time implied by patient's equilibrium beliefs and current waitlist lengths. True pref. rank of requested GP is the rank of a patient's requested GP in their true flow payoff ordering. This table is referenced in Section V.E.  $^{\dagger}$ By normalization.

Figure A.1. HelseNorge Screenshots

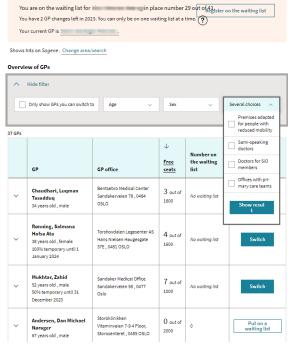
(a) Sorted Alphabetically

(b) Sorted by Free Seats

#### Change GP ?



#### Change GP ?



Notes: The figure shows two screenshots from the "Change GP" (bytte fastlege) tool on Norway's centralized online health platform, HelseNorge. The page shows the list of 37 GPs located in the Sagene neighborhood of Oslo. Panel (a) sorts this list alphabetically by GP last name (the default), and panel (b) sorts the list by the number of free slots available on each GP's panel. Only three GPs have available slots on their panel. (Webpage translated from Norwegian to English using Google Chrome, which slightly affects the rendering of graphics relative to the original.) Accessed August 18, 2023; available at https://tjenester.helsenorge.no/bytte-fastlege?fylke=03&kommuner=0301&bydeler=030103. This figure is referenced at footnote 15.

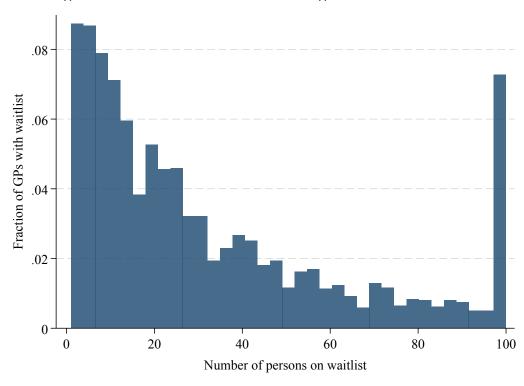


Figure A.2. Distribution of Waitlist lengths in December 2019

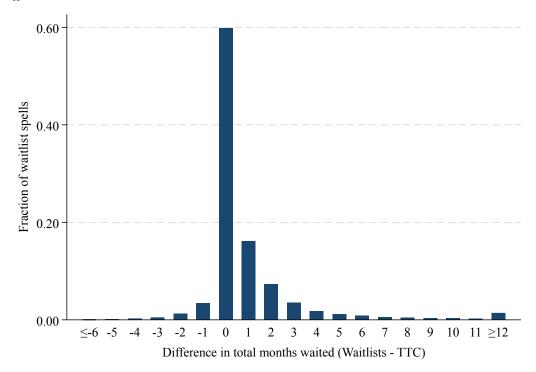
Notes: The figure shows the distribution of waiting list lengths in Norway in December 2019, among GPs that had a waiting list. Waitlist length is top-coded at 100 for readability. There were  $3{,}695$  unique GPs with waiting lists (out of  $5{,}010$  total GPs). This figure is referenced in footnote 22.

Table A.1. Patient Demographics by Outcome of Running TTC in December 2019

	Full	Not	On a	a waitlist
Sample demographic	Sample	on a waitlist	Reassigned	Not reassigned
Number of individuals	4,573,170	4,463,532	18,667	90,971
Pct. of individuals		0.98	0.00	0.02
Demographics				
Pct. female	0.50	0.49	0.66	0.66
Age	47	47	42	41
Years of education	13.1	13.1	13.4	13.3
Annual income (000 NOK)	413	414	397	373
Pct. temporary resident	0.07	0.07	0.04	0.12
Pct. ever moved	0.11	0.10	0.24	0.24
Choice of GP				
Pct. ever switched to open GP	0.13	0.13	0.17	0.30
Travel time to current GP (min.)	10.8	10.7	15.8	14.5
Pct. with GP of same gender	0.58	0.58	0.55	0.53
Use of waitlists				
Pct. ever on a waitlist	0.09	0.07	1.00	1.00
Number of months on a waitlist $  > 0$	6.4	4.9	7.9	10.7
Pct. waiting for GP of same gender	0.64	0.64	0.65	0.65
Travel time to wl. GP – curr. GP (min.)	-6.8	-7.2	-8.4	-5.6

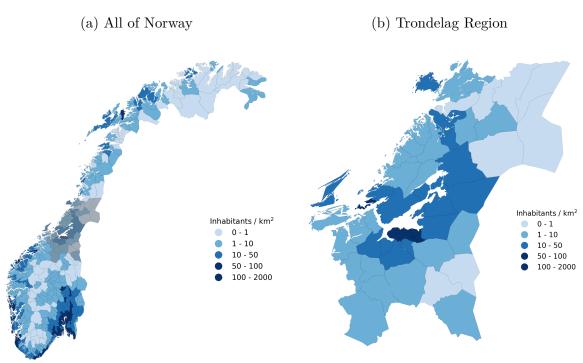
Notes: The table provides summary statistics on adult patients based on the outcome of running TTC on waitlists as of December 2019. Summary statistics for each individual are calculated based on the time period 2017–2019, not just as they were observed in December 2019. "Ever" means at any point during 2017–2019. The first column reports means among all adult patients in the population. The remaining three columns are a partition of patients based on whether they were not standing on a waitlist in December 2019 and thus did not participate in TTC ("Not on a waitlist"), whether they were on a waitlist and were successfully reassigned by the TTC algorithm ("On a waitlist/Reassigned"), and finally those patients who were on a waitlist but were not successfully reassigned via TTC. This table is referenced in Section II.C.





Notes: The figure shows the distribution of waiting time differences that result from the simple mechanical simulation of TTC using the historical waitlist data. An observation is a waitlist spell. The figure reports the difference between the number of months the patient waited under the status quo mechanism (Waitlists) and that under the TTC mechanism (TTC). While most patients wait for less time under TTC, 4.5 percent of patients wait for longer. This figure is referenced in Section II.C.

Figure A.4. Population Density Map



Notes: The figure shows a population density map of all of Norway as well as just the Trondelag region. In panel (a), the Trondelag region is shaded in gray. The outlined shapes within the map are municipalities. There are 421 municipalities in Norway and 58 in Trondelag (using 2019 region boundaries). The population center of Trondelag (the city Trondheim) lies at the center of the region in the darkest shaded municipality. This figure is referenced in footnote 30.

Table A.2. Comparison of Norway and Trondelag Region, 2019

Sample demographic	All of Norway	Trondelag
Panel A. Patient characteristics		
Number of individuals	4,633,395	412,774
Demographics		
Pct. female	0.50	0.49
Age	48	47
Pct. with post-secondary education	0.32	0.31
Annual income (000 NOK)	429	403
Pct. temporary resident	0.07	0.07
Pct. ever moved	0.04	0.06
Choice of GP		
Pct. ever switched to open GP	0.05	0.05
Travel time to current GP (min.)	10.7	10.9
Pct. with GP of same gender	0.58	0.57
Use of waitlists		
Pct. ever on a waitlist	0.05	0.05
Number of months on a waitlist $  > 0$	5.0	4.9
Pct. waiting for GP of same gender	0.64	0.65
Travel time to wl. GP – curr. GP (min.)	-6.7	-7.9
Panel B. GP characteristics		
Number of GP panels	5,549	474
Panel characteristics		
Enrollment cap	1,120	1,078
Pct. months with available slots	0.32	0.27
Pct. months with temporary GP	0.12	0.12
GP demographics		
Pct. female	0.43	0.46
Pct. rural	0.37	0.52
Age	47	45
Panel enrollment stats.		
Num. waiting on waitlist	24	22
Num. enrollees / cap	0.94	0.97

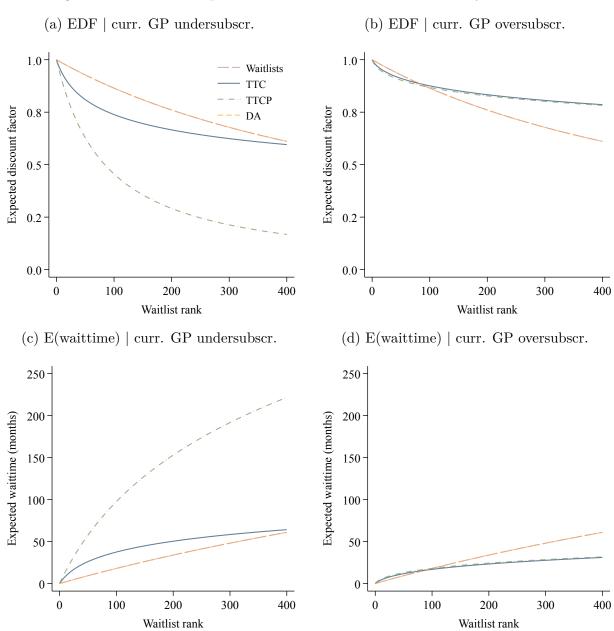
Notes: The table compares descriptive statistics between all of Norway and the Trondelag region in 2019. Panel A reports statistics on (adult) patients, and all values represent means over patient-months. "Ever" means at any point during 2019. Moves are counted only if they are across municipalities. Age, gender, education, and income data are not available for temporary residents, so those means are only among permanent residents. Panel B reports statistics on GPs, and all values in the table represent means over GP panel-months. GP enrollment and waitlist use statistics reflect the full population (including children under 16). This table is referenced in Section IV.A.

Table A.3. Summary Statistics on Realizations from Exogenous Processes

	Mean	SD
Number of patients	371,536	_
Number of attention shocks received	2,299	47
Number of moves	773	28
Number of aging shocks	735	26
Number of deaths	428	21
Number of moves in past 6 months	6,102	332
Number of attn. shocks in past 12 months	28,393	2,506

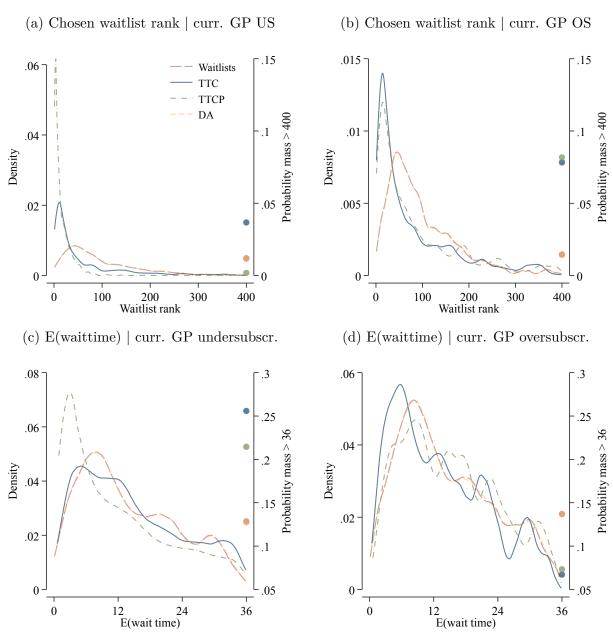
Notes: The table describes the realizations of exogenous processes in our simulated economy. These include the demographic transition processes (patients aging, dying, and moving) and the attention process (patients receiving attention shocks). Patients that die are immediately reborn, so there are a fixed number of patients in all periods. Statistics in the table are calculated across the 500 periods in the simulation. This table is referenced in section V.A.

Figure A.5. Relationship Between Beliefs and Waitlist Rank by Mechanism



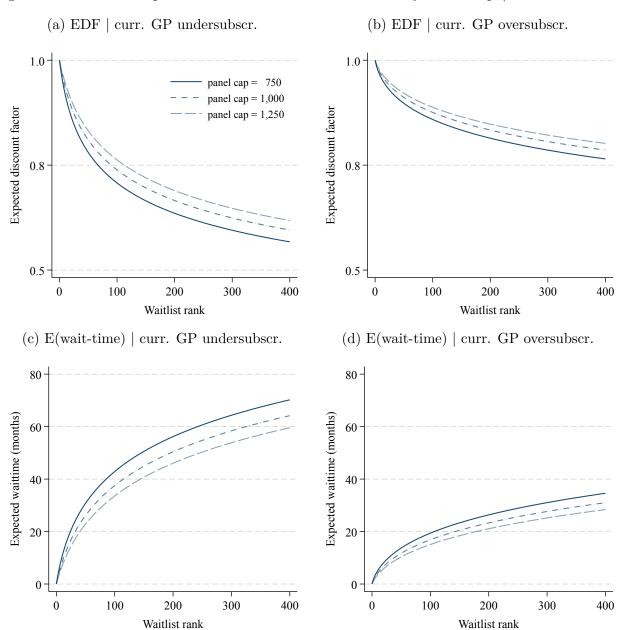
Notes: The figure shows the relationship between beliefs and waitlist rank across our four focal mechanisms, supposing all waitlists were for a GP with a panel cap of 1,000. Panels (a) and (b) report a patient's expected discount factor (EDF) as a function of waitlist rank. Panel (a) shows the EDF for a patient whose current GP is undersubscribed, while panel (b) shows the EDF for a patient whose current GP is oversubscribed. Panels (c) and (d) show the corresponding expected waiting times. This figure is referenced in Appendix D.2.

Figure A.6. Distribution of Chosen Waitlist Lengths by Mechanism



Notes: The figure shows the distribution of chosen waitlist ranks and the corresponding expected waiting times among attentive patients in each of our focal mechanisms. Panels (a) and (b) report the distribution of attentive patients' chosen waitlist rank conditional on being less than 400. The dots (scaled on the right axis) report the probability mass above this truncation point. Panels (c) and (d) report the distribution of corresponding expected waiting times, conditional on being below 36 months. Again, the dots (scaled on the right axis) report the probability mass above the truncation point. This figure is referenced in Appendix D.2.

Figure A.7. Relationship Between Beliefs and Waitlist Rank by Panel Cap (TTC Mechanism)



Notes: The figure shows the relationship between patient beliefs and waitlist rank for three different GP panel cap sizes, under the TTC mechanism. Panels (a) and (b) report a patient's expected discount factor (EDF) as a function of waitlist rank, if the waitlist considered was for a GP with a panel cap of 750, 1,000, or 1,250. Panel (a) shows the EDF for a patient whose current GP is undersubscribed, while panel (b) shows the EDF for a patient whose current GP is oversubscribed. Panels (c) and (d) show the corresponding expected waiting times. A higher panel capacity will make the waitlist move faster, and thus expected wait-time lower (and EDF higher). If a patient's current GP is oversubscribed, they will understand that they have the possibility of being reassigned via TTC, and thus have more optimistic expectations about waiting time. This figure is referenced in Appendix D.2.